Static and dynamic analysis: synergy and duality

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Goals

Theme:

- Static and dynamic analyses are more similar than many people believe

- One person's view of their relationship

Goals:

- Encourage blending of the techniques and communities

- Start productive discussions

Outline

Review of static and dynamic analysis

Synergy: combining static and dynamic analysis

- Aggregation
- Analogies
- Hybrids

Duality: subsets of behavior

Conclusion

Static analysis

Examples: compiler optimizations, program verifiers

Examine program text (no execution)

Build a model of program state

- An abstraction of the run-time state

Reason over possible behaviors

- E.g., "run" the program over the abstract state

Abstract interpretation

Typically implemented via dataflow analysis

Each program statement's *transfer function* indicates how it transforms state

Example: What is the transfer function for

```
y = x++;
```

?

Selecting an abstract domain

$\langle$ x is odd; y is odd $\rangle$

`y = x++;`

$\langle$ x is even; y is odd $\rangle$

$\langle$ x is prime; y is prime $\rangle$

`y = x++;`

$\langle$ x is anything; y is prime $\rangle$

$\langle$ x = { 3, 5, 7 }; y = { 9, 11, 13 } $\rangle$

`y = x++;`

$\langle$ x = { 4, 6, 8 }; y = { 3, 5, 7 } $\rangle$

$\langle x=3, y=11\rangle, \langle x=5, y=9\rangle, \langle x=7, y=13\rangle$

`y = x++;`

$\langle x=4, y=3\rangle, \langle x=6, y=5\rangle, \langle x=8, y=7\rangle$

$\langle$ $x_n = f(a_{n-1},\ldots,z_{n-1})$; $y_n = f(a_{n-1},\ldots,z_{n-1})$ $\rangle$

`y = x++;`

$\langle$ $x_{n+1} = x_n+1$; $y_{n+1} = x_n$ $\rangle$

Research challenge: Choose good abstractions

The abstraction determines the expense (in time and space)

The abstraction determines the accuracy (what information is lost)

- Less accurate results are poor for applications that require precision

- Cannot conclude all true properties in the grammar

Static analysis recap

- Slow to analyze large models of state, so use abstraction

- Conservative: account for abstracted-away state

- Sound: (weak) properties are guaranteed to be true

  *Some static analyses are not sound

Dynamic analysis

Examples: profiling, testing

Execute program (over some inputs)
- The compiler provides the semantics

Observe executions
- Requires instrumentation infrastructure

Must choose what to measure, and what test runs

Research challenge:
What to measure?

Coverage or frequency

- Statements, branches, paths, procedure calls, types, method dispatch

Values computed

- Parameters, array indices

Run time, memory usage

Test oracle results

Similarities among runs [Podgurski 99, Reps 97]

Like abstraction, determines what is reported

Research challenge: Choose good tests

The test suite determines the expense (in time and space)

The test suite determines the accuracy (what executions are never seen)

- Less accurate results are poor for applications that require correctness
- Many domains do not require correctness!

*What information is being collected also matters

Dynamic analysis recap

- Can be as fast as execution (over a test suite, and allowing for data collection)
  - Example: aliasing
- Precise: no abstraction or approximation
- Unsound: results may not generalize to future executions
  - Describes execution environment or test suite

Static analysis

Abstract domain
   slow if precise

Conservative

   due to abstraction

Sound

   due to conservatism

Dynamic analysis

Concrete execution
   slow if exhaustive

Precise

   no approximation

Unsound

   does not generalize

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Combining static and dynamic analysis

1. Aggregation:
   Pre- or post-processing

2. Inspiring analogous analyses:
   Same problem, different domain

3. Hybrid analyses:
   Blend both approaches

1. Aggregation: Pre- or post-processing

Use output of one analysis as input to another

Dynamic then static

- Profile-directed compilation: unroll loops, inline, reorder dispatch, …
- Verify properties observed at run time

Static then dynamic

- Reduce instrumentation requirements
  - Efficient branch/path profiling
  - Discharge obligations statically (type/array checks)
- Type checking (e.g., Java, including generics)
- Indicate suspicious code to test more thoroughly

2. Analogous analyses: Same problem, different domain

Any analysis problem can be solved in either domain

- Type safety: no memory corruption or operations on wrong types of values
  - Static type-checking
  - Dynamic type-checking
- Slicing: what computations could affect a value
  - Static: reachability over dependence graph
  - Dynamic: tracing

Memory checking

Goal: find array bound violations, uses of uninit. memory

Purify [Hastings 92]: run-time instrumentation
- Tagged memory: 2 bits (allocated, initialized) per byte
- Each instruction checks/updates the tags
  - Allocate: set "A" bit, clear "I" bit
  - Write: require "A" bit, set "I" bit
  - Read: require "I" bit
  - Deallocate: clear "A" bit

LCLint [Evans 96]: compile-time dataflow analysis
- Abstract state contains allocated and initialized bits
- Each transfer function checks/updates the state

Identical analyses!

Another example: atomicity checking [Flanagan 2003]

Specifications

- Specification checking
  - Statically: theorem-proving
  - Dynamically: `assert` statement

- Specification generation
  - Statically: by hand or abstract interpretation [Cousot 77]
  - Dynamically: by invariant detection [Ernst 99], reporting unfalsified properties

Your analogous analyses here

Look for gaps with no analogous analyses!

Try using the same analysis

- But be open to completely different approaches

There is still low-hanging fruit to be harvested

3. Hybrid analyses: Blending static and dynamic

Combine static and dynamic analyses

- Not mere aggregation, but a new analysis
- Disciplined trade-off between precision and soundness: find the sweet spot between them

Possible starting points

Analyses that trade off run-time and precision

- Different abstractions (at different program points)
- Switch between static and dynamic at analysis time

Ignore some available information

- Examine only some paths [Evans 94, Detlefs 98, Bush 00]

Merge based on observation that both examine only a subset of executions (next section of talk)

- Problem: optimistic vs. pessimistic treatment

More examples: (bounded) model checking, security analyses, delta debugging [Zeller 99], etc.

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   does not generalize

Sound dynamic analysis

Observe every possible execution!

Problem: infinite number of executions

Solution: test case selection and generation

- Efficiency tweaks to an algorithm that works perfectly in theory but exhausts resources in practice

Precise static analysis

Reason over full program state!

Problem: infinite number of executions

Solution: data or execution abstraction

- Efficiency tweaks to an algorithm that works perfectly in theory [Cousot 77] but exhausts resources in practice

Dynamic analysis focuses on a subset of executions

The executions in the test suite

- Easy to enumerate
- Characterizes program use

Typically optimistic for other executions

Static analysis focuses on a subset of data structures

More precise for data or control described by the abstraction

- Concise logical description
- Typically conservative elsewhere (safety net)

Example: k-limiting [Jones 81]

- Represents each object reachable by $\leq k$ pointers
- Groups together (approximates) more distant objects

Dual views of subsets

Execution and data subsets are views on the same space

Every execution subset corresponds to a data subset

- Executions induce data structures and control flow

Every data subset corresponds to an execution subset

- A set of objects represents the executions that generate them

Subset description may be concise in one domain but complex in the other

- What if the test suite was generated from a specification?

Any analysis may be conservative over other behaviors

Differences between the approaches

Static and dynamic analysis communities work with different subsets

- Each subset and characterization is better for certain uses

What subsets have a concise description in both domains?

- Augment a test suite to fill out the data structures that it creates, making the data structure description a smaller logical formula

A hybrid view of subsets

Bring together static and dynamic analysis by unifying their subset descriptions

- Find subsets with small descriptions with respect to both data structures and executions
- Find a new, smaller description

Advantages of this approach

- Directly compare previous disparate analyses
- Directly apply analyses to other domain
- Switch between the approaches
- Obtain insight in order to devise and optimize analyses

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Potential pitfalls

Analogies between analyses

- What applications tolerate unsoundness/imprecision?
- Any more low-hanging fruit?
- Most static and dynamic approaches differ

Hybrid analyses

- How to measure and trade off precision and soundness
  - What is "partial soundness"? What is in between?
- Not all static analyses are abstract interpretation
- Optimistic vs. pessimistic treatment of unseen executions

Subset characterization

- Find the unified characterization of behavior

Conclusion

Static and dynamic analysis share many similarities

- Communities should be closer

Create analogous analyses

- Many successes so far

Hybrid approach holds great promise

- Analyses increasingly look like points in this continuum
- Unified theory of subsets of executions/data is key

(Our) future work: explore this space