

Lang  
FUZZ

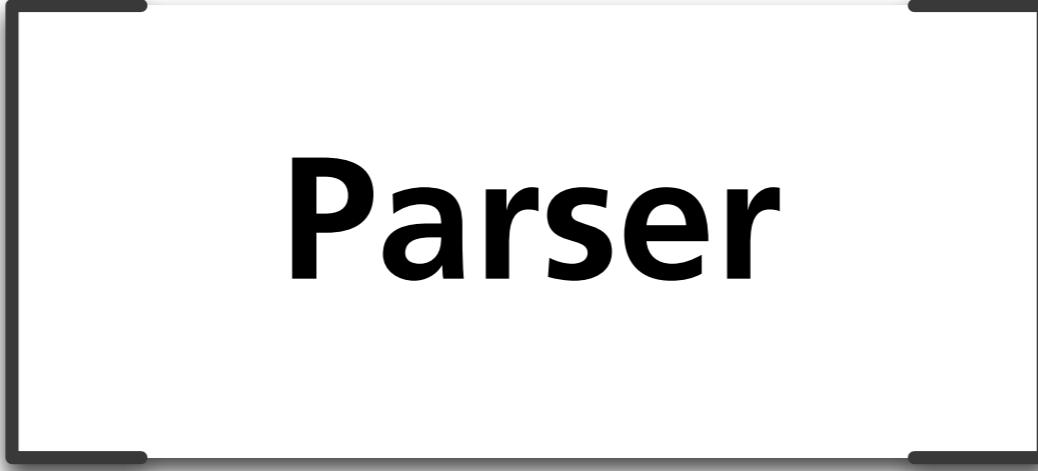
# Grammar-Based Fuzzing

Security Testing

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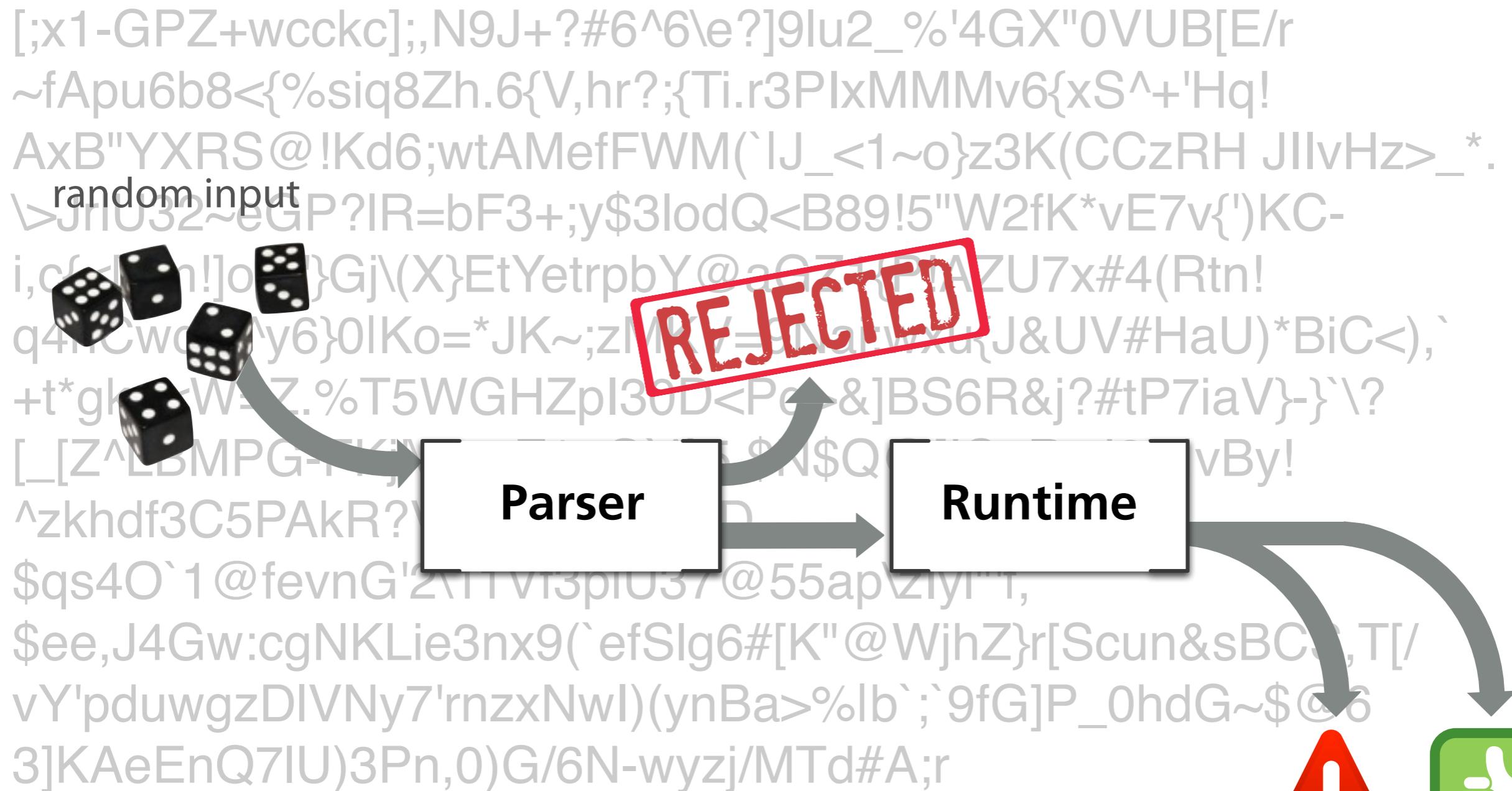
# Grammar Fuzzing

- Suppose you want to test a *parser* – to compile and execute a program

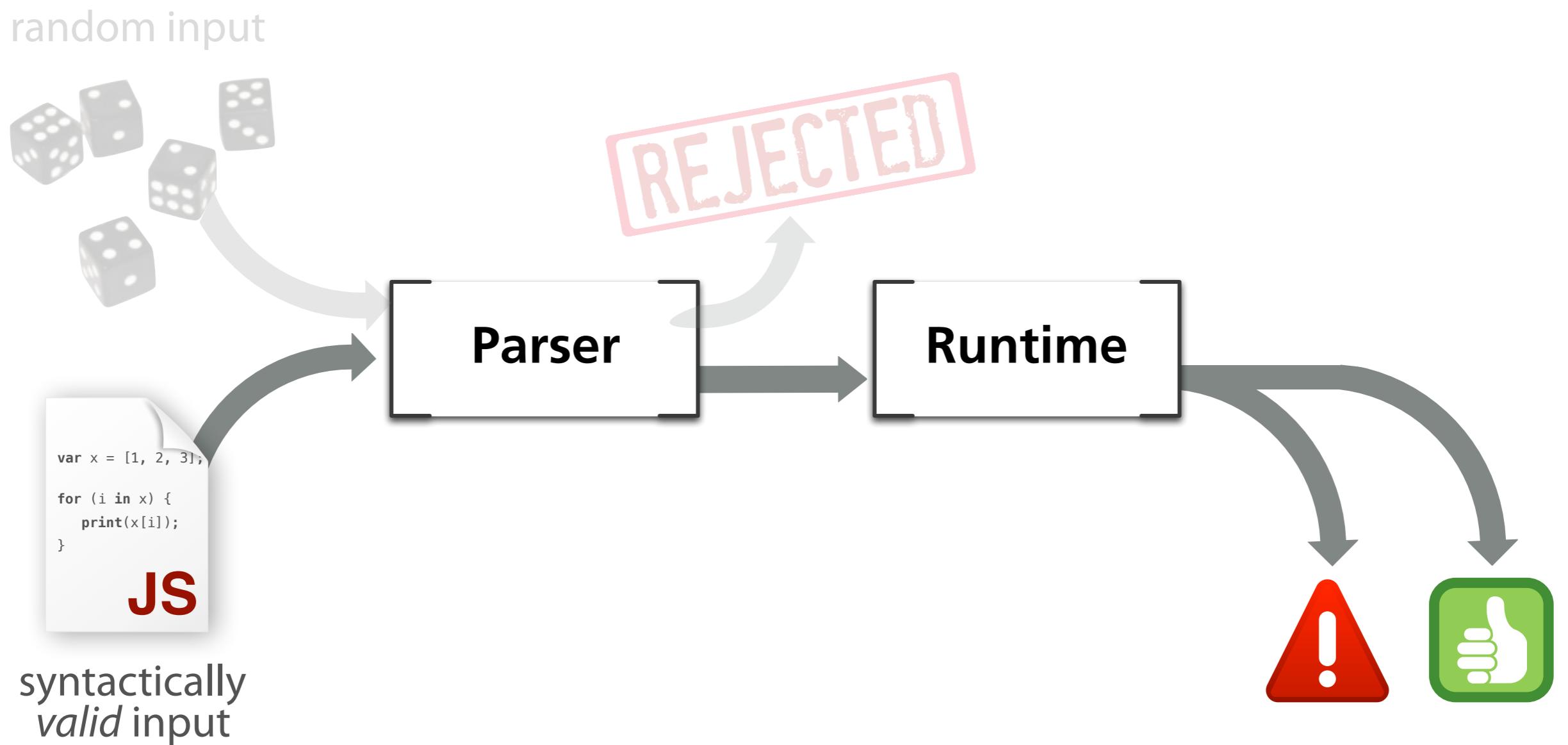


Parser

# Grammar Fuzzing



# Grammar Fuzzing

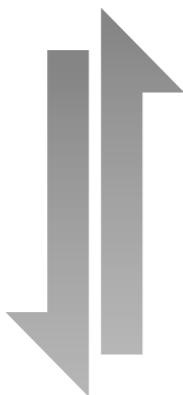


# LangFuzz



- Fuzz tester using a full-fledged *grammar* to generate inputs
- Can be parametrized with a *grammar*
- Can use grammar to *parse existing inputs*

# JavaScript as Domain



- If an attacker gains control over the *JavaScript interpreter*, he gains control over the *entire browser*

# JavaScript Grammar

Fuzzing  
JavaScript

Sample  
Code

Language  
Grammar



Mutated Test



Test Driver

Test  
Suite



# JavaScript Grammar

## If Statement

*IfStatement<sup>full</sup>* ⇒

| **if** ParenthesizedExpression Statement<sup>full</sup>  
| **if** ParenthesizedExpression Statement<sup>noShortIf</sup> **else** Statement<sup>full</sup>

*IfStatement<sup>noShortIf</sup>* ⇒ **if** ParenthesizedExpression Statement<sup>noShortIf</sup> **else** Statement<sup>noShortIf</sup>

## Switch Statement

*SwitchStatement* ⇒

| **switch** ParenthesizedExpression { }  
| **switch** ParenthesizedExpression { CaseGroups LastCaseGroup }

*CaseGroups* ⇒

«empty»

| CaseGroups CaseGroup

*CaseGroup* ⇒ CaseGuards BlockStatementsPrefix

*LastCaseGroup* ⇒ CaseGuards BlockStatements

*CaseGuards* ⇒

CaseGuard

| CaseGuards CaseGuard

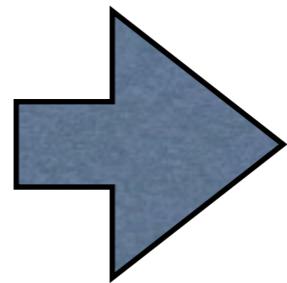
*CaseGuard* ⇒

# A Generated Input

---

```
1 var haystack = "foo";
2 var re_text = "^foo";
3 haystack += "x";
4 re_text += "(x)";
5 var re = new RegExp(re_text);
6 re.test(haystack);
7 RegExp.input = Number();
8 print(RegExp.$1);
```

---



# Fuzzing with Grammars

- Want to encode a *grammar* to produce arithmetic expressions as *strings*
- \$START expands into \$EXPR, which can expand into \$TERM, \$TERM + \$TERM, etc.

# Fuzzing with Grammars

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```
$START    ::= $EXPR
$EXPR     ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM      ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR   ::= +$FACTOR | -$FACTOR | ($EXPR) |
              $INTEGER | $INTEGER.$INTEGER
$INTEGER  ::= $INTEGER$DIGIT | $DIGIT
$DIGIT    ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Fuzzing with Grammars

\$START



```
$START    ::= $EXPR
$EXPR     ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM     ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR   ::= +$FACTOR | -$FACTOR | ($EXPR) |
              $INTEGER | $INTEGER.$INTEGER
$INTEGER  ::= $INTEGER$DIGIT | $DIGIT
$DIGIT    ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Fuzzing with Grammars

\$EXPR



```
$START   ::= $EXPR
$EXPR    ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM    ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR  ::= +$FACTOR | -$FACTOR | ($EXPR) |
             $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT   ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Fuzzing with Grammars

**\$EXPR + \$TERM**



```
$START   ::= $EXPR
$EXPR    ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM    ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR  ::= +$FACTOR | -$FACTOR | ($EXPR) |
             $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT   ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Fuzzing with Grammars

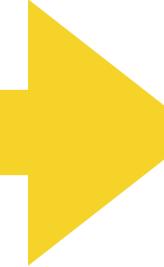
**\$EXPR + \$FACTOR**



```
$START ::= $EXPR
$EXPR ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR ::= +$FACTOR | -$FACTOR | ($EXPR) |
           $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Fuzzing with Grammars

**\$TERM + \$FACTOR**



```
$START ::= $EXPR
$EXPR ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR ::= +$FACTOR | -$FACTOR | ($EXPR) |
           $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Fuzzing with Grammars

\$FACTOR + \$FACTOR



```
$START   ::= $EXPR
$EXPR    ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM    ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR  ::= +$FACTOR | -$FACTOR | ($EXPR) |
             $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT   ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Fuzzing with Grammars

\$FACTOR + \$INTEGER



```
$START   ::= $EXPR
$EXPR    ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM    ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR  ::= +$FACTOR | -$FACTOR | ($EXPR) |
             $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT   ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Fuzzing with Grammars

**\$INTEGER + \$INTEGER**



```
$START    ::= $EXPR
$EXPR     ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM      ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR   ::= +$FACTOR | -$FACTOR | ($EXPR) |
              $INTEGER | $INTEGER.$INTEGER
$INTEGER  ::= $INTEGER$DIGIT | $DIGIT
$DIGIT    ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Fuzzing with Grammars

**\$DIGIT + \$INTEGER**

```
$START    ::= $EXPR
$EXPR     ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM      ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR   ::= +$FACTOR | -$FACTOR | ($EXPR) |
              $INTEGER | $INTEGER.$INTEGER
$INTEGER  ::= $INTEGER$DIGIT | $DIGIT
$DIGIT    ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```



# Fuzzing with Grammars

2 + \$INTEGER



```
$START   ::= $EXPR
$EXPR    ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM    ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR  ::= +$FACTOR | -$FACTOR | ($EXPR) |
             $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT   ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Fuzzing with Grammars

$$2 + 2 \quad \checkmark$$

```
$START    ::= $EXPR
$EXPR     ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM      ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR   ::= +$FACTOR | -$FACTOR | ($EXPR) |
              $INTEGER | $INTEGER.$INTEGER
$INTEGER  ::= $INTEGER$DIGIT | $DIGIT
$DIGIT    ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Automatic Production

- Implement production in Python
- Start with \$START, apply rules randomly

```
#!/usr/bin/env python
# Grammar-based Fuzzing

import random

term_grammar = {
    "$START":
        ["$EXPR"],

    "$EXPR":
        ["$EXPR + $TERM", "$EXPR - $TERM", "$TERM"],

    "$TERM":
        ["$TERM * $FACTOR", "$TERM / $FACTOR", "$FACTOR"],

    "$FACTOR":
        ["+$FACTOR", "-$FACTOR", "($EXPR)", "$INTEGER",
    "$INTEGER.$INTEGER"],

    "$INTEGER":
        ["$INTEGER$DIGIT", "$DIGIT"],

    "$DIGIT":
        ["0", "1", "2", "3", "4", "5", "6", "7", "8", "9"]
}
```

# Grammar Encoding

Demo

# grammar-fuzz.py

- Want to encode a *grammar* to produce arithmetic expressions as *strings*
- \$START expands into \$EXPR, which can expand into \$TERM, \$TERM + \$TERM, etc.

```
#!/usr/bin/env python
# Grammar-based Fuzzing
```

```
import random
```

```
term_grammar = {
    "$START": [
        "$EXPR",
```

```
#!/usr/bin/env python
# Grammar-based Fuzzing

import random

term_grammar = {
    "$START":
        ["$EXPR"],

    "$EXPR":
        ["$EXPR + $TERM", "$EXPR - $TERM", "$TERM"],

    "$TERM":
        ["$TERM * $FACTOR", "$TERM / $FACTOR", "$FACTOR"],

    "$FACTOR":
        ["+$FACTOR", "-$FACTOR", "($EXPR)", "$INTEGER",
    "$INTEGER.$INTEGER"],

    "$INTEGER":
        ["$INTEGER$DIGIT", "$DIGIT"],

    "$DIGIT":
        ["0", "1", "2", "3", "4", "5", "6", "7", "8", "9"]
}
```

```
"$EXPR":  
    ["$EXPR + $TERM", "$EXPR - $TERM", "$TERM"],  
  
"$TERM":  
    ["$TERM * $FACTOR", "$TERM / $FACTOR", "$FACTOR"],  
  
"$FACTOR":  
    ["+$FACTOR", "-$FACTOR", "($EXPR)", "$INTEGER",  
"$INTEGER.$INTEGER"],  
  
"$INTEGER":  
    ["$INTEGER$DIGIT", "$DIGIT"],  
  
"$DIGIT":  
    ["0", "1", "2", "3", "4", "5", "6", "7", "8", "9"]  
}
```

```
def apply_rule(term, rule):  
    (old, new) = rule  
    # We replace the first occurrence;  
    # this could also be some random occurrence  
    return term.replace(old, new, 1)
```

```
MAX_SYMBOLS = 5  
MAX_TRIES = 500
```

```
def produce(grammar):
    term = "$START"
    tries = 0

    while term.count('$') > 0:
        # All rules have the same chance;
        # this could also be weighted
        key = random.choice(grammar.keys())
        repl = random.choice(grammar[key])
        new_term = apply_rule(term, (key, repl))
        if new_term != term and new_term.count('$') <
MAX_SYMBOLS:
            term = new_term
            tries = 0
        else:
            tries += 1
            if tries >= MAX_TRIES:
                assert False, "Cannot expand " + term

    return term

if __name__ == "__main__":
    print(produce(html_grammar))
```

```
$EXPR
$EXPR - $TERM
$EXPR + $TERM - $TERM
$EXPR + $TERM * $FACTOR - $TERM
$TERM + $TERM * $FACTOR - $TERM
$TERM + $TERM * -$FACTOR - $TERM
$FACTOR + $TERM * -$FACTOR - $TERM
-$FACTOR + $TERM * -$FACTOR - $TERM
--$FACTOR + $TERM * -$FACTOR - $TERM
--$FACTOR + $FACTOR * -$FACTOR - $TERM
--$FACTOR + $FACTOR * -$FACTOR - $FACTOR
--+$FACTOR + $FACTOR * -$FACTOR - $FACTOR
--+$FACTOR + $FACTOR * -$FACTOR - $FACTOR
--+$IN
----+--2 + 3.5 * -+1 - +5
--+$DIGIT
--+2 +
--+2 + $INTEGER.$INTEGER * -$FACTOR - $FACTOR
--+2 + $INTEGER.$INTEGER * -+$FACTOR - $FACTOR
--+2 + $INTEGER.$INTEGER * -+$INTEGER - $FACTOR
--+2 + $DIGIT.$INTEGER * -+$INTEGER - $FACTOR
--+2 + 3.$INTEGER * -+$INTEGER - $FACTOR
--+2 + 3.$INTEGER * -+$INTEGER - +$FACTOR
--+2 + 3.$INTEGER * -+$INTEGER - +$INTEGER
--+2 + 3.$DIGIT * -+$INTEGER - +$INTEGER
--+2 + 3.5 * -+$INTEGER - +$INTEGER
--+2 + 3.5 * -+$DIGIT - +$INTEGER
--+2 + 3.5 * -+1 - +$INTEGER
--+2 + 3.5 * -+1 - +$DIGIT
--+2 + 3.5 * -+1 - +5
```

# Grammar Coverage

- Idea: Want to *cover* as many rules as possible
- Approach: Save that expansion has been applied (*covered*)
- Prefer *uncovered* over *covered* expansions

# Grammar Coverage

\$START



```
$START   ::= $EXPR
$EXPR    ::= $EXPR + $TERM | $EXPR - $TERM | $TERM
$TERM    ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR  ::= +$FACTOR | -$FACTOR | ($EXPR) |
             $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT   ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Grammar Coverage

\$EXPR



\$START ::= \$EXPR ✓  
\$EXPR ::= \$EXPR + \$TERM | \$EXPR - \$TERM | \$TERM  
\$TERM ::= \$TERM \* \$FACTOR | \$TERM / \$FACTOR | \$FACTOR  
\$FACTOR ::= +\$FACTOR | -\$FACTOR | (\$EXPR) |  
              \$INTEGER | \$INTEGER.\$INTEGER  
\$INTEGER ::= \$INTEGER\$DIGIT | \$DIGIT  
\$DIGIT ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

# Grammar Coverage

**\$EXPR + \$TERM**



```
$START ::= $EXPR✓
$EXPR  ::= $EXPR + $TERM✓ | $EXPR - $TERM | $TERM
$TERM   ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR
$FACTOR ::= +$FACTOR | -$FACTOR | ($EXPR) |
           $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT  ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Grammar Coverage

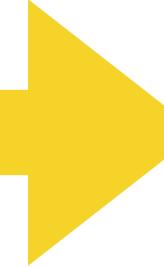
**\$EXPR + \$FACTOR**



```
$START ::= $EXPR✓
$EXPR ::= $EXPR + $TERM✓ | $EXPR - $TERM | $TERM
$TERM ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR✓
$FACTOR ::= +$FACTOR | -$FACTOR | ($EXPR) |
           $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Grammar Coverage

**\$TERM + \$FACTOR**



```
$START ::= $EXPR✓
$EXPR ::= $EXPR + $TERM✓ | $EXPR - $TERM | $TERM✓
$TERM ::= $TERM * $FACTOR | $TERM / $FACTOR | $FACTOR✓
$FACTOR ::= +$FACTOR | -$FACTOR | ($EXPR) |
           $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Grammar Coverage

**\$TERM \* \$FACTOR + \$FACTOR**



```
$START ::= $EXPR✓
$EXPR ::= $EXPR + $TERM✓ | $EXPR - $TERM | $TERM✓
$TERM ::= $TERM * $FACTOR✓ | $TERM / $FACTOR | $FACTOR✓
$FACTOR ::= +$FACTOR | -$FACTOR | ($EXPR) |
           $INTEGER | $INTEGER.$INTEGER
$INTEGER ::= $INTEGER$DIGIT | $DIGIT
$DIGIT ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Grammar Coverage

**\$TERM \* \$INTEGER + \$FACTOR**



```
$START ::= $EXPR✓  
$EXPR ::= $EXPR + $TERM✓ | $EXPR - $TERM | $TERM✓  
$TERM ::= $TERM * $FACTOR✓ | $TERM / $FACTOR | $FACTOR✓  
$FACTOR ::= +$FACTOR | -$FACTOR | ($EXPR) |  
          $INTEGER✓ | $INTEGER.$INTEGER  
$INTEGER ::= $INTEGER$DIGIT | $DIGIT  
$DIGIT ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Grammar Coverage

**\$TERM \* \$DIGIT + \$FACTOR**

\$START ::= \$EXPR   
\$EXPR ::= \$EXPR + \$TERM  | \$EXPR - \$TERM | \$TERM   
\$TERM ::= \$TERM \* \$FACTOR  | \$TERM / \$FACTOR | \$FACTOR   
\$FACTOR ::= +\$FACTOR | -\$FACTOR | (\$EXPR) |  
              \$INTEGER  | \$INTEGER.\$INTEGER  
\$INTEGER ::= \$INTEGER\$DIGIT | \$DIGIT   
\$DIGIT ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9



# Grammar Coverage

**\$TERM \* 2 + \$FACTOR**



```
$START ::= $EXPR✓  
$EXPR ::= $EXPR + $TERM✓ | $EXPR - $TERM | $TERM✓  
$TERM ::= $TERM * $FACTOR✓ | $TERM / $FACTOR | $FACTOR✓  
$FACTOR ::= +$FACTOR | -$FACTOR | ($EXPR) |  
          $INTEGER✓ | $INTEGER.$INTEGER  
$INTEGER ::= $INTEGER$DIGIT | $DIGIT✓  
$DIGIT ::= 0 | 1 | 2✓ | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# Grammar Coverage

**\$TERM \* 2 + \$INTEGER. \$INTEGER**

\$START	::= \$EXPR
\$EXPR	::= \$EXPR + \$TERM    \$EXPR - \$TERM   \$TERM
\$TERM	::= \$TERM * \$FACTOR    \$TERM / \$FACTOR   \$FACTOR
\$FACTOR	::= +\$FACTOR   -\$FACTOR   (\$EXPR)   \$INTEGER    \$INTEGER. \$INTEGER
\$INTEGER	::= \$INTEGER\$DIGIT   \$DIGIT
\$DIGIT	::= 0   1   2    3   4   5   6   7   8   9



# Grammar Coverage

$\$TERM * 2 + \$INTEGER\$DIGIT.\$INTEGER$

\$START ::= \$EXPR   
\$EXPR ::= \$EXPR + \$TERM  | \$EXPR - \$TERM | \$TERM   
\$TERM ::= \$TERM \* \$FACTOR  | \$TERM / \$FACTOR | \$FACTOR   
\$FACTOR ::= +\$FACTOR | -\$FACTOR | (\$EXPR) |  
              \$INTEGER  | \$INTEGER.\$INTEGER   
\$INTEGER ::= \$INTEGER\$DIGIT  | \$DIGIT   
\$DIGIT ::= 0 | 1 | 2  | 3 | 4 | 5 | 6 | 7 | 8 | 9



# Grammar Coverage

$\$TERM * 2 + \$DIGIT\$DIGIT.\$INTEGER$

$\$START$	$::= \$EXPR \checkmark$
$\$EXPR$	$::= \$EXPR + \$TERM \checkmark \mid \$EXPR - \$TERM \mid \$TERM \checkmark$
$\$TERM$	$::= \$TERM * \$FACTOR \checkmark \mid \$TERM / \$FACTOR \mid \$FACTOR \checkmark$
$\$FACTOR$	$::= +\$FACTOR \mid -\$FACTOR \mid (\$EXPR) \mid$ $\quad \$INTEGER \checkmark \mid \$INTEGER.\$INTEGER \checkmark$
$\$INTEGER$	$::= \$INTEGER\$DIGIT \checkmark \mid \$DIGIT \checkmark$
$\$DIGIT$	$::= 0 \mid 1 \mid 2 \checkmark \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$



# Grammar Coverage

\$TERM \* 2 + 5\$DIGIT.\$INTEGER

\$START ::= \$EXPR   
\$EXPR ::= \$EXPR + \$TERM  | \$EXPR - \$TERM | \$TERM   
\$TERM ::= \$TERM \* \$FACTOR  | \$TERM / \$FACTOR | \$FACTOR   
\$FACTOR ::= +\$FACTOR | -\$FACTOR | (\$EXPR) |  
              \$INTEGER  | \$INTEGER.\$INTEGER   
\$INTEGER ::= \$INTEGER\$DIGIT  | \$DIGIT   
\$DIGIT ::= 0 | 1 | 2  | 3 | 4 | 5  | 6 | 7 | 8 | 9



# Grammar Coverage

\$TERM \* 2 + 56. \$INTEGER

```
$START   ::= $EXPR✓
$EXPR    ::= $EXPR + $TERM✓ | $EXPR - $TERM | $TERM✓
$TERM    ::= $TERM * $FACTOR✓ | $TERM / $FACTOR | $FACTOR✓
$FACTOR  ::= +$FACTOR | -$FACTOR | ($EXPR) |
             $INTEGER✓ | $INTEGER. $INTEGER✓
$INTEGER ::= $INTEGER$DIGIT✓ | $DIGIT✓
$DIGIT   ::= 0 | 1 | 2✓ | 3 | 4 | 5✓ | 6✓ | 7 | 8 | 9
```

# Grammar Coverage

-8 / +7 \* 2 + 56.9



```
$START   ::= $EXPR✓  
$EXPR    ::= $EXPR + $TERM✓ | $EXPR - $TERM | $TERM✓  
$TERM    ::= $TERM * $FACTOR✓ | $TERM / $FACTOR✓ | $FACTOR✓  
$FACTOR  ::= +$FACTOR✓ | -$FACTOR✓ | ($EXPR) |  
           $INTEGER✓ | $INTEGER.$INTEGER✓  
$INTEGER ::= $INTEGER$DIGIT✓ | $DIGIT✓  
$DIGIT   ::= 0 | 1 | 2✓ | 3 | 4 | 5✓ | 6✓ | 7 | 8 | 9✓
```

# Tracking Coverage

- Track coverage in Python
- Mark used productions as "covered"
- Prefer uncovered productions over covered ones

Demo

# Things To Do

- Don't apply rules randomly;  
instead, find those that can be applied
- Prefer uncovered *rules* over covered ones
- Prefer rules that *lead* to uncovered ones
- Cover not only single rules, but *pairs*  
(triples? paths?) of expansions
- Produce *multiple outputs*,  
preserving coverage