

# Fault-based testing

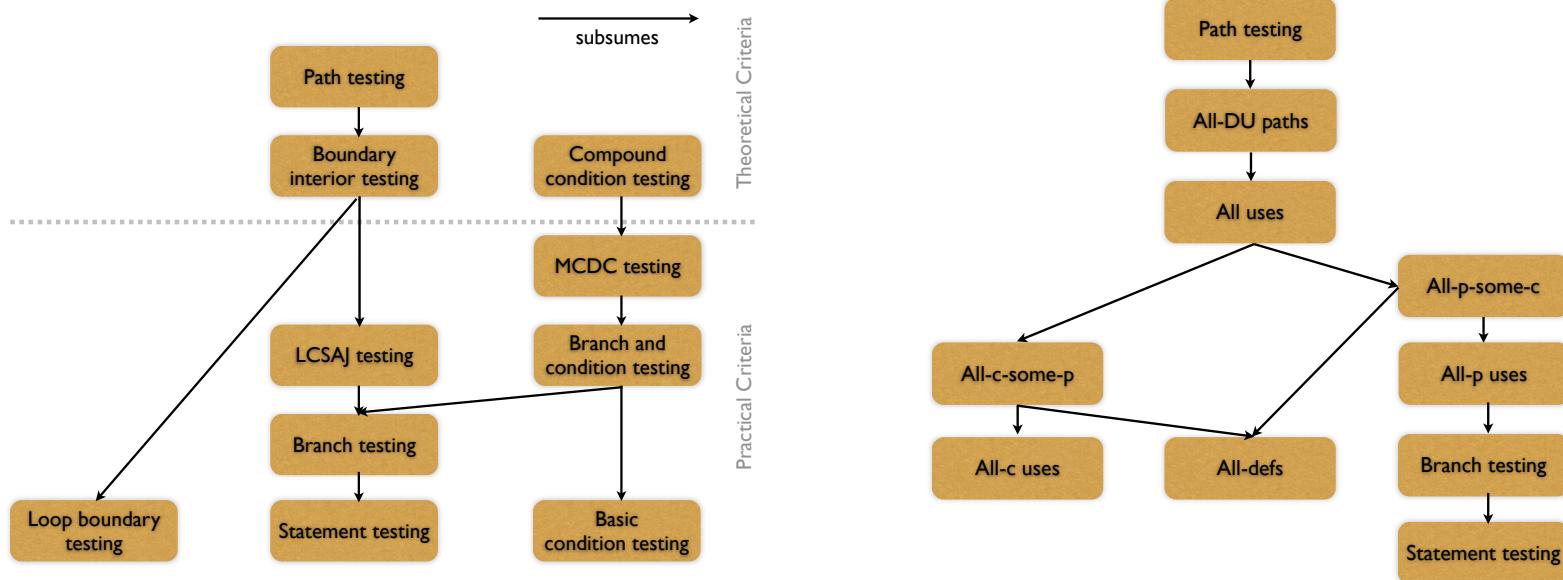
Automated testing and  
verification

J.P. Galeotti - Alessandra Gorla

slides by Gordon Fraser

# How good are my tests?

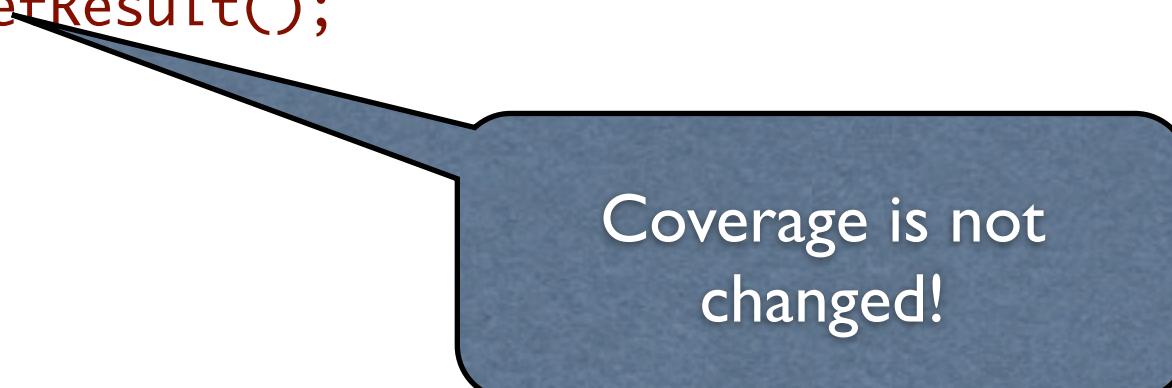
# How good are my tests?



```
/**  
 * Make sure Double.NaN is returned iff n = 0  
 *  
 */  
public void testNaN() {  
    StandardDeviation std = new StandardDeviation();  
    assertTrue(Double.isNaN(std.getResult()));  
    std.increment(1d);  
    assertEquals(0d, std.getResult(), 0);  
}
```

```
/**  
 * Make sure Double.NaN is returned iff n = 0  
 *  
 */  
public void testNaN() {  
    StandardDeviation std = new StandardDeviation();  
    Double.isNaN(std.getResult());  
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    std.getResult();  
}
```

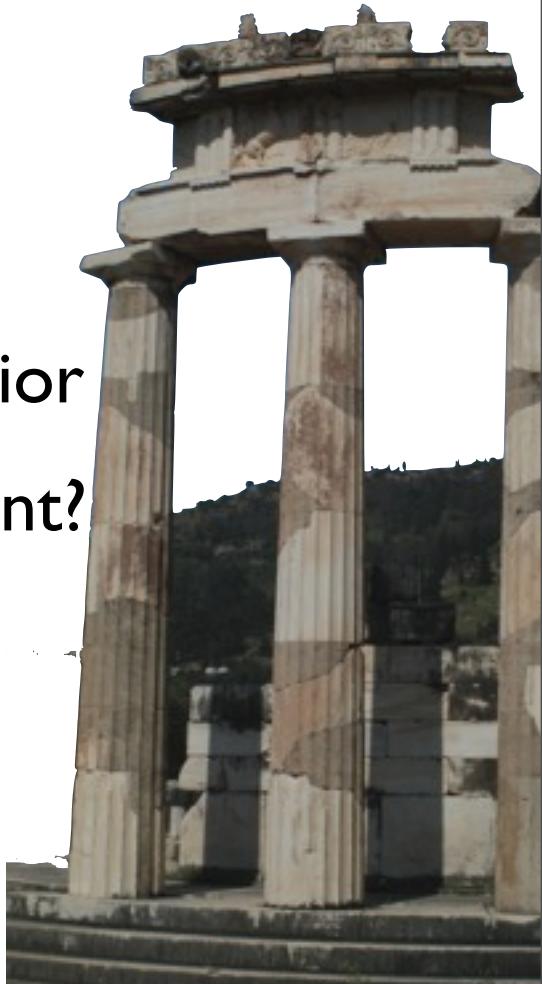
```
/**  
 * Make sure Double.NaN is returned iff n = 0  
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 */  
public void testNaN() {  
    StandardDeviation std = new StandardDeviation();  
    Double.isNaN(std.getResult());  
    std.increment(1d);  
    std.getResult();  
}
```



Coverage is not  
changed!

# The Oracle Problem

- Executing all the code is not enough
- We need to check the functional behavior
- Does this thing actually do what we want?



# Test Oracles

- Formal specifications
- Code assertions
- Test assertions
- Code contracts
- Manual oracles

# How good are my tests?

- Coverage = how much of the code is executed
- But how much of the code is checked?
- We don't know where the bugs are
- But we know the bugs we have made in the past!

# Learning from Mistakes

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- **Key idea:** Learning from earlier mistakes to prevent them from happening again

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- **Key technique:** *Simulate earlier mistakes* and see whether the resulting defects are found

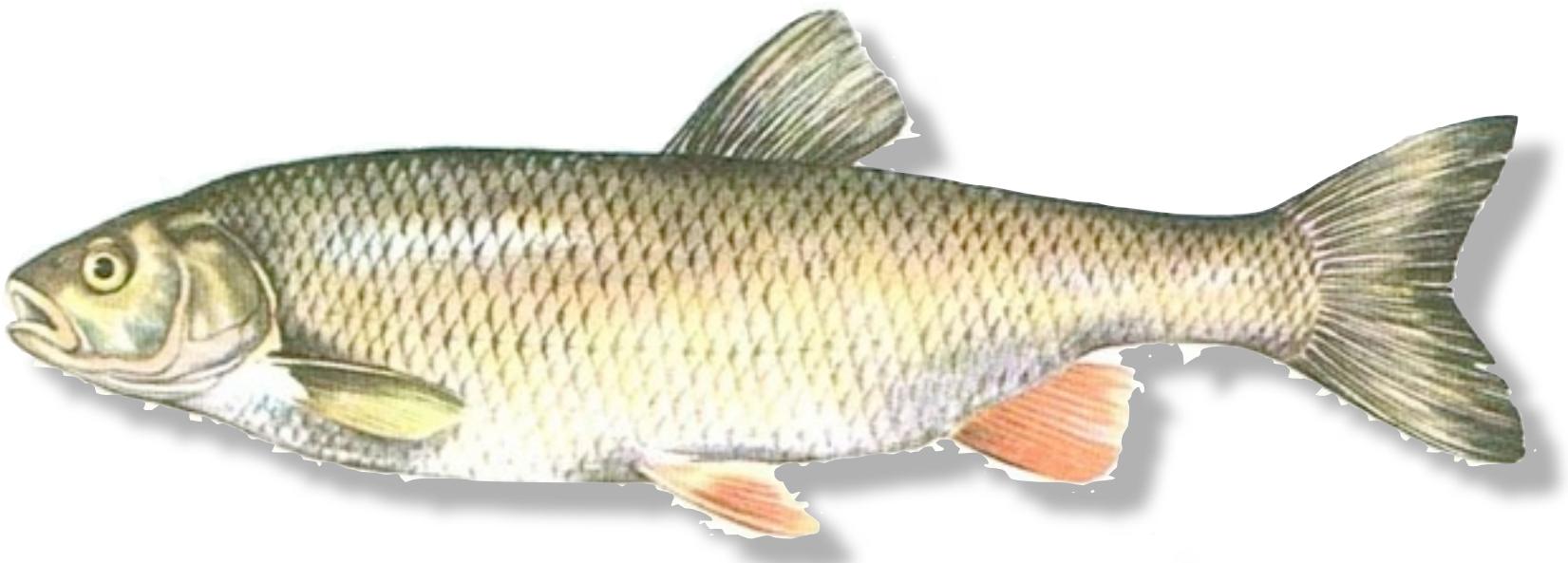
# Learning from Mistakes

- **Key idea:** Learning from earlier mistakes to prevent them from happening again
- **Key technique:** *Simulate earlier mistakes* and see whether the resulting defects are found
- Known as *fault-based testing* or *mutation testing*



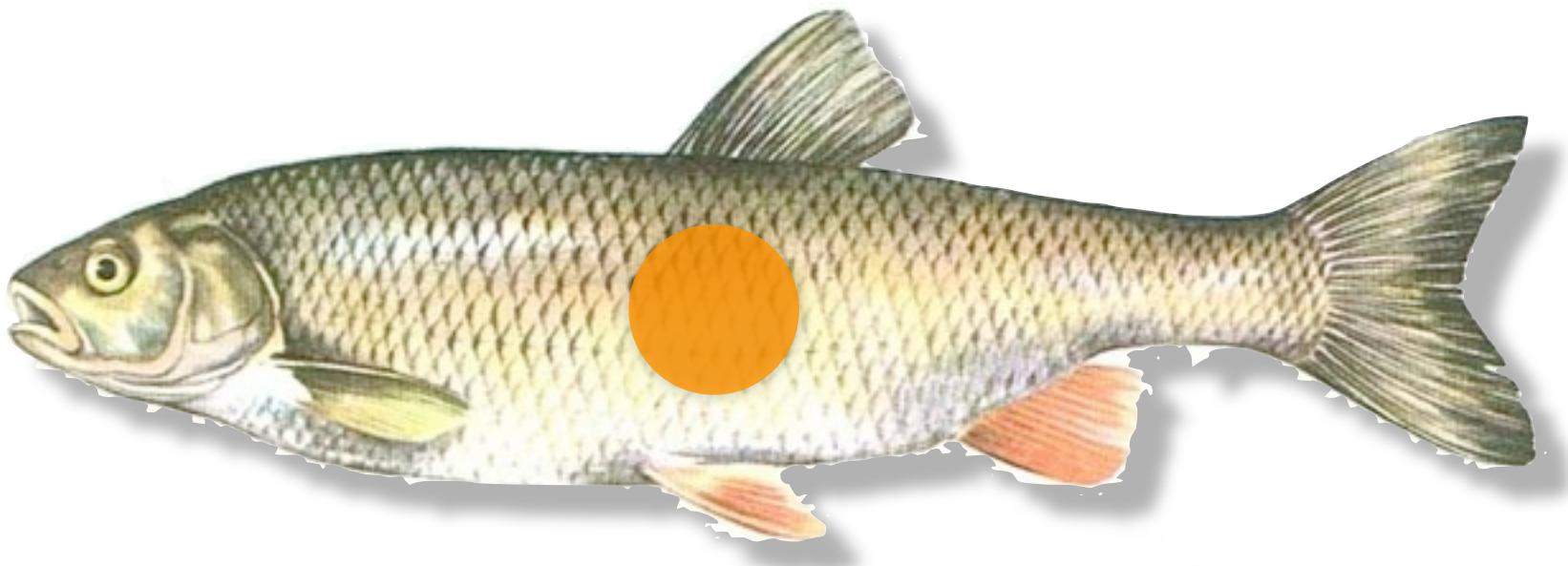
Thursday, January 17, 13

# Fish Tag



- We catch 100 fish and tag them

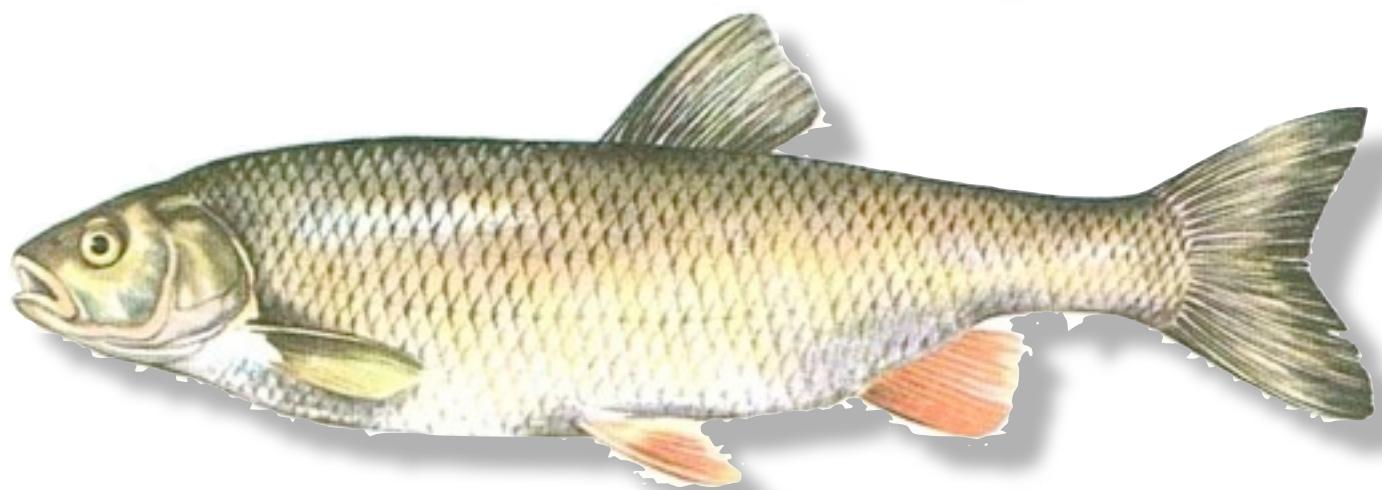
# Fish Tag



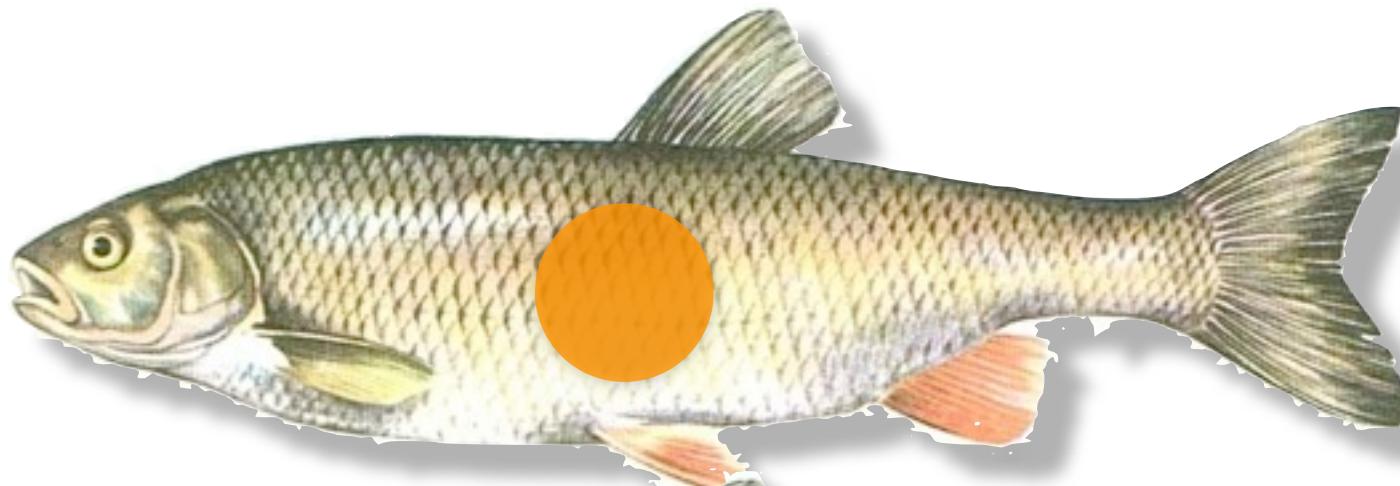
- We catch 100 fish and tag them

# Counting Tags

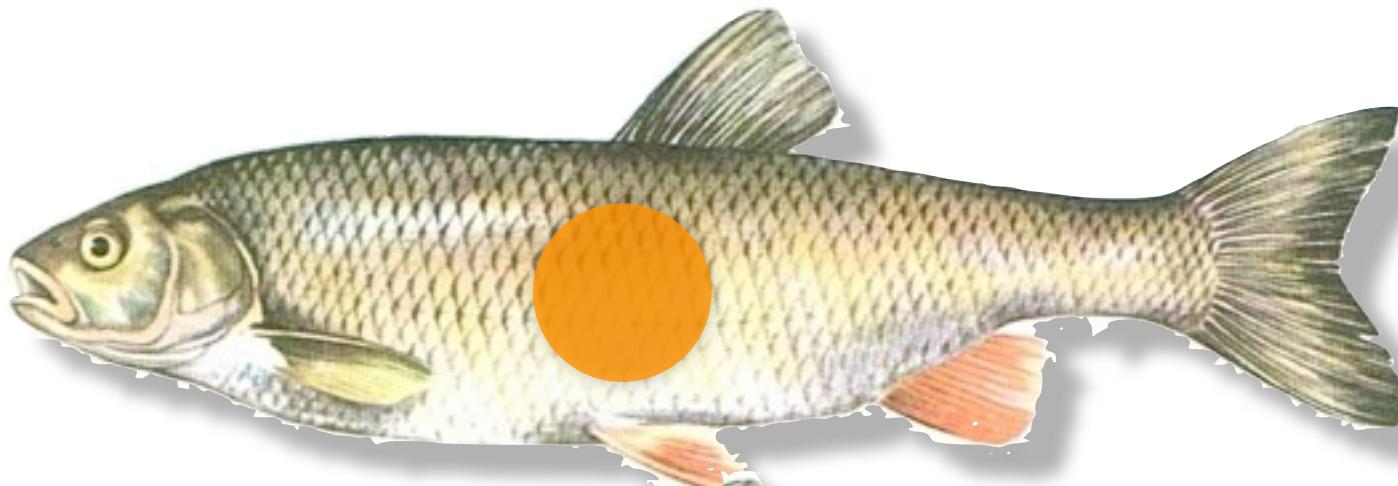
# Counting Tags



# Counting Tags



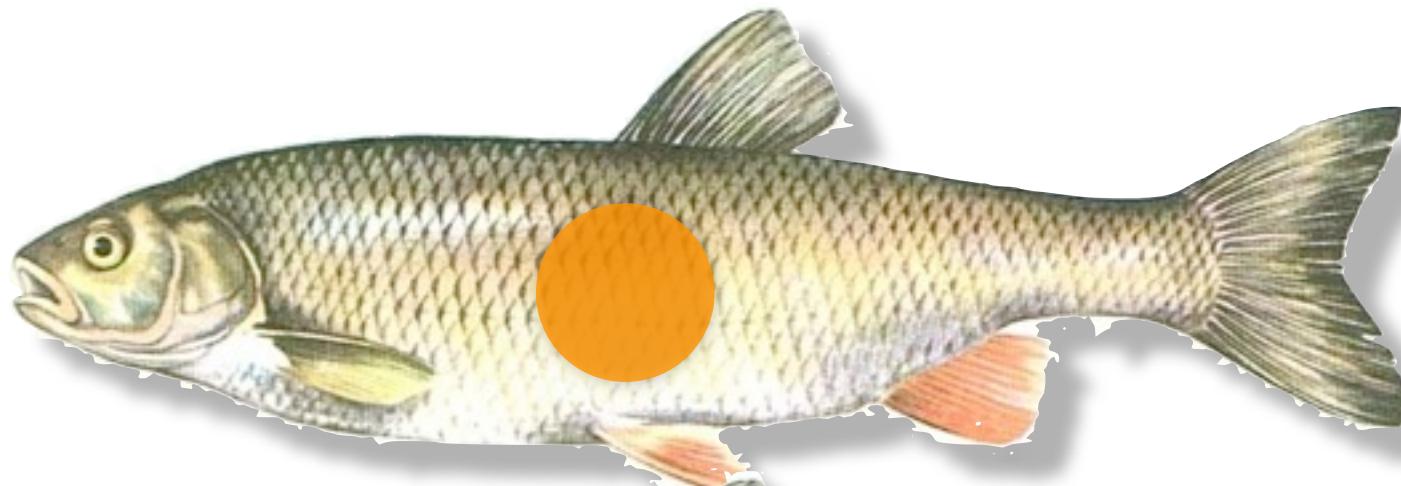
# Counting Tags



80

# Counting Tags

20



80

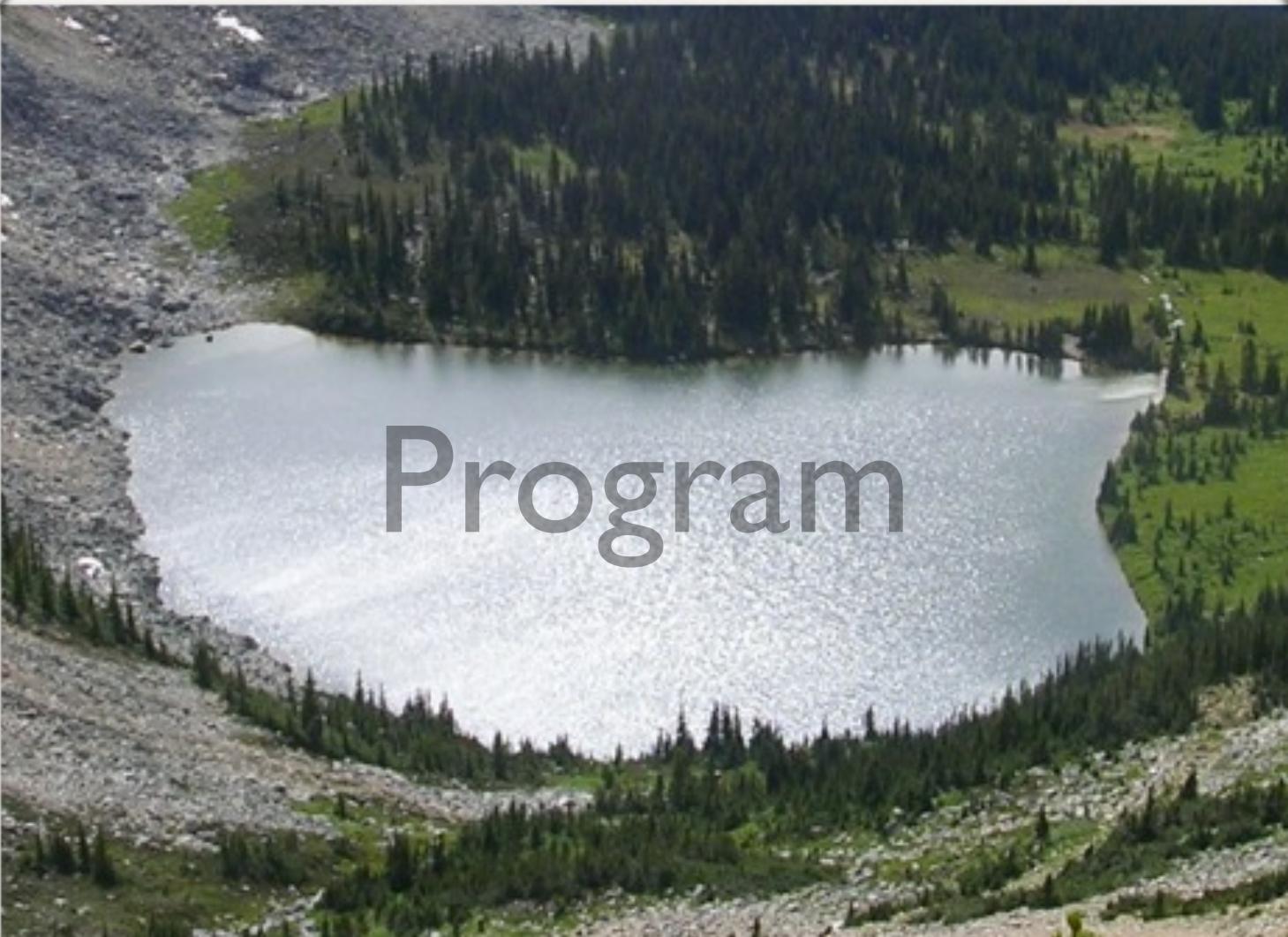


# Estimate

$$\frac{100}{\text{untagged fish population}} = \frac{20}{80}$$

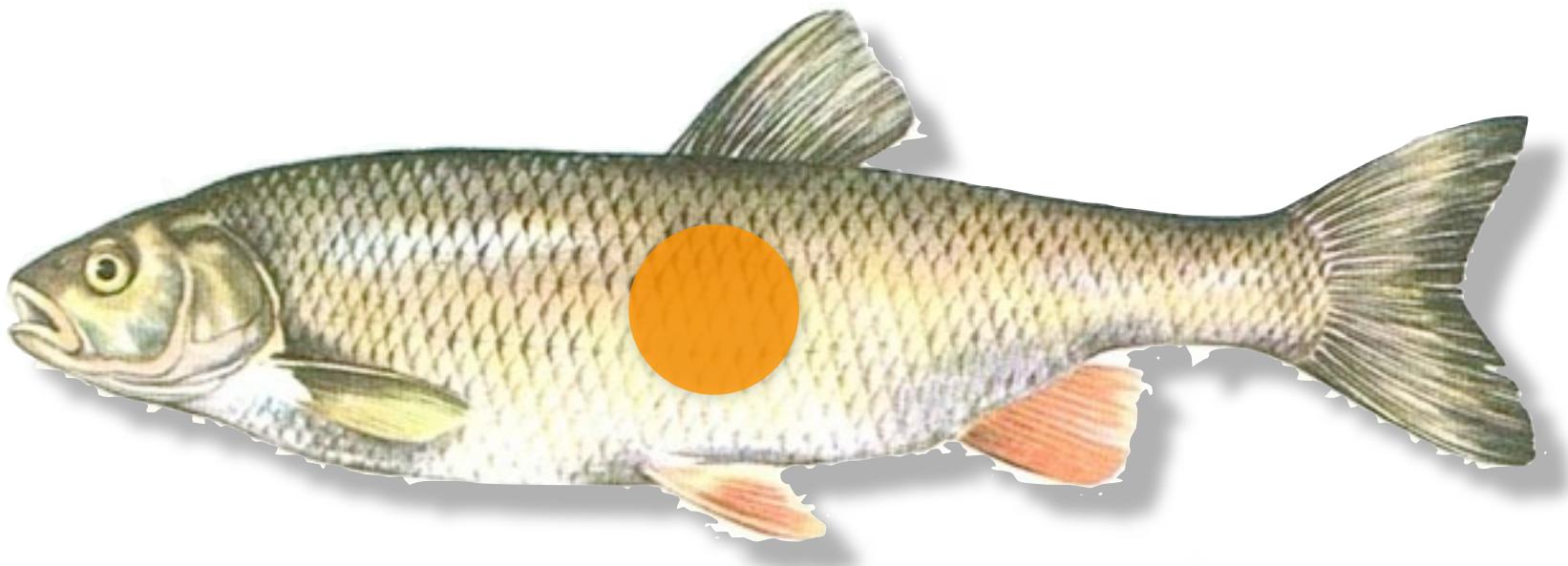


Thursday, January 17, 13



# Program

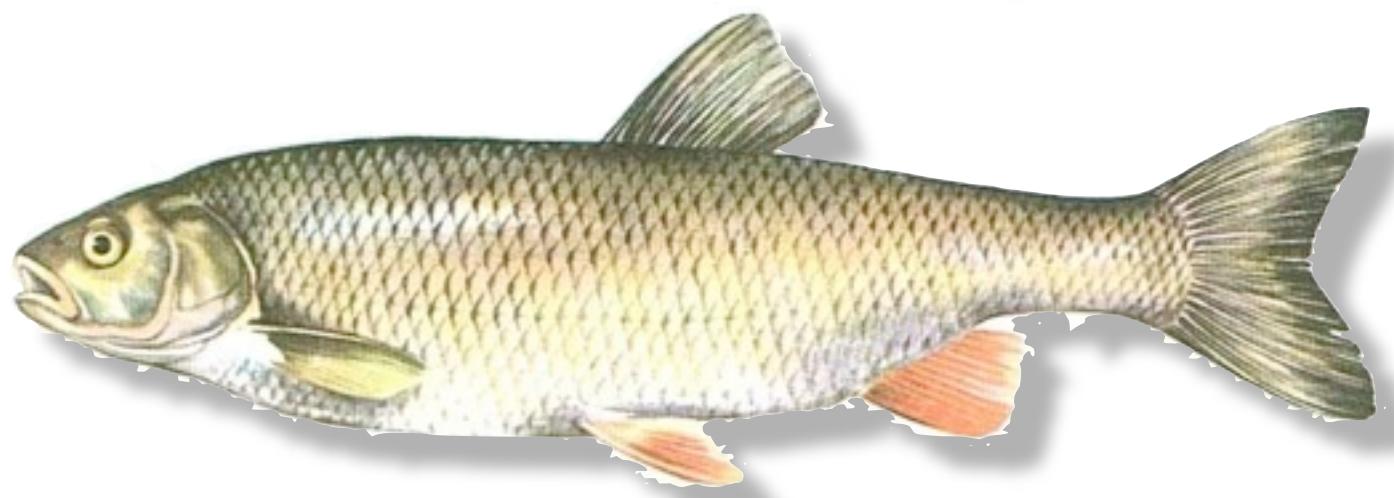
# A Mutant



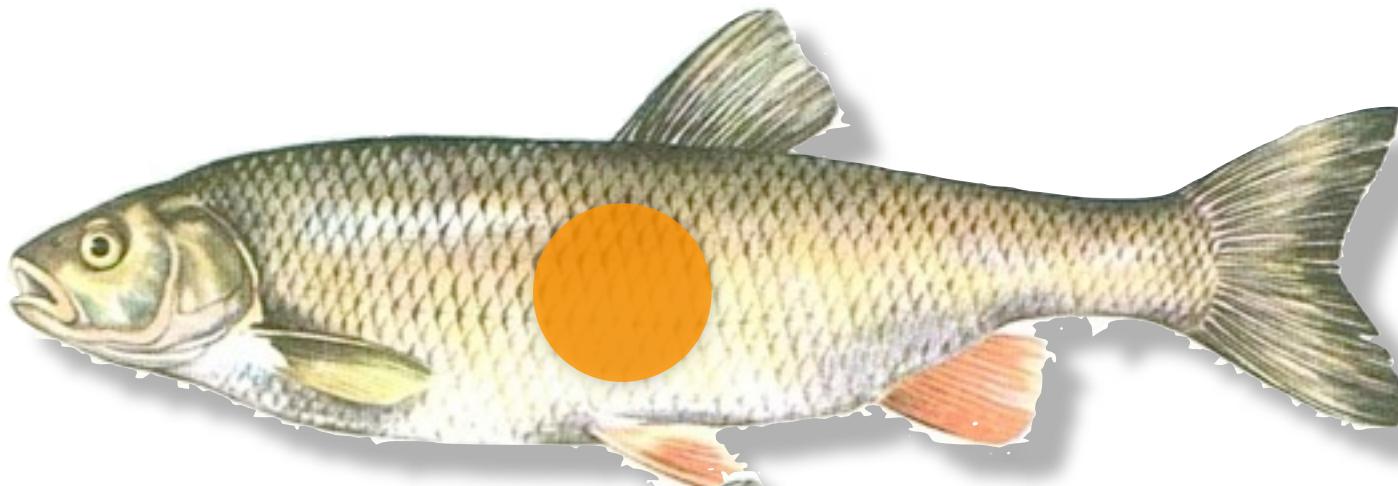
- We seed 100 mutations into the program

# Counting Mutants

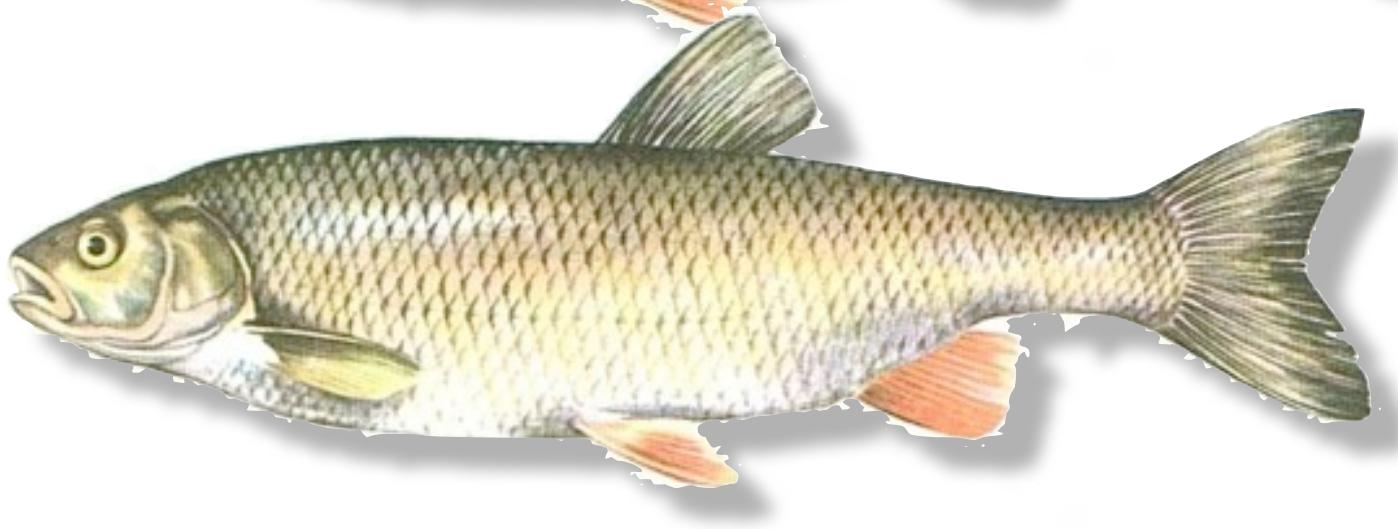
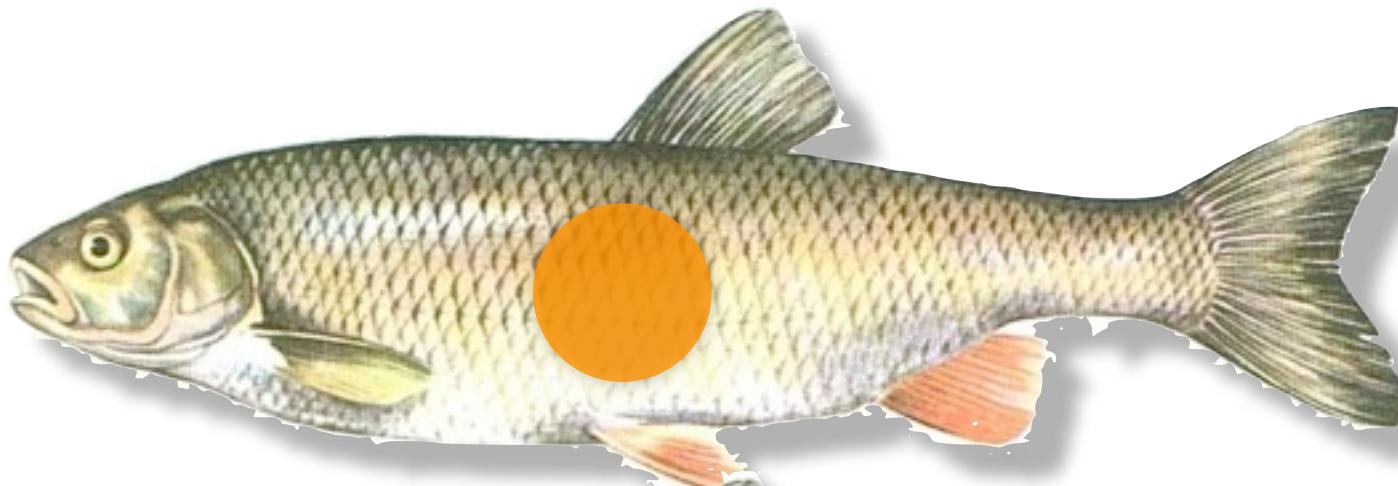
# Counting Mutants



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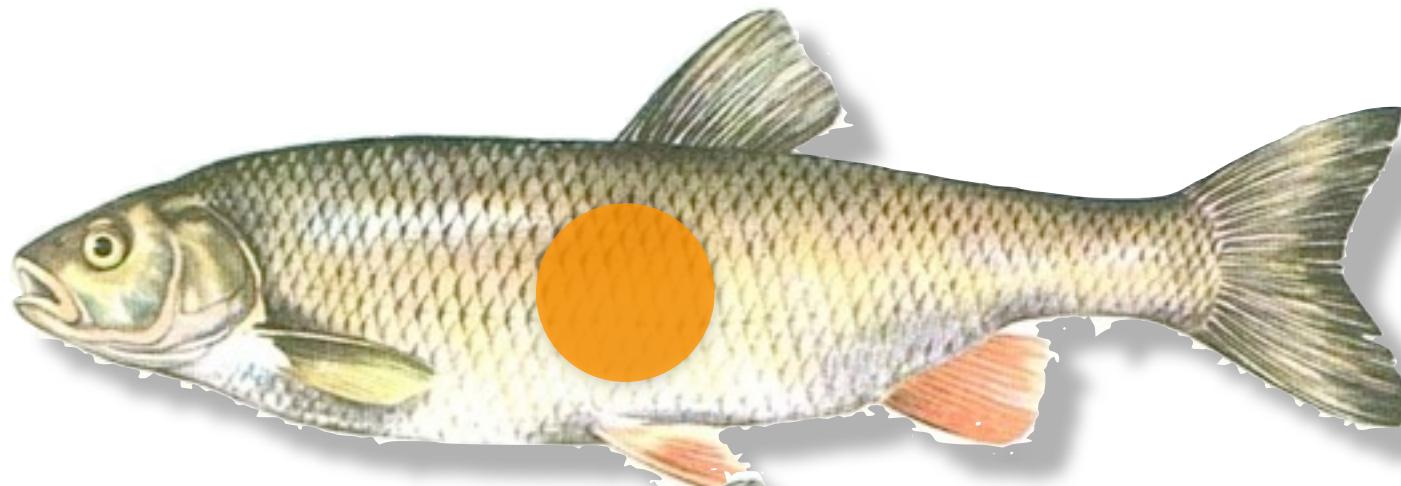
# Counting Mutants



80

# Counting Mutants

20



80



# Estimate

$$\frac{100}{\text{remaining defects}} = \frac{20}{80}$$

# Basic Assumptions

- Judge effectiveness of a test suite in finding real faults, by measuring how well it finds seeded fake faults.
- Valid to the extent that the seeded bugs are representative of real bugs
- Not necessarily identical (e.g., tagged fish not identical to non tagged fish); but the differences should not affect the selection

```
int do_something(int x, int  
y) {  
    if(x < y)  
        return x+y;  
    else  
        return x*y;  
}
```

## Program

```
int do_something(int x, int  
y) {  
    if(x < y)  
        return x+y;  
    else  
        return x*y;  
}
```

## Program

```
int a = do_something(5,  
10);  
assertEquals(a, 15);
```

Test

```
int do_something(int x, int  
y) {  
    if(x < y)  
        return x+y;  
    else  
        return x*y;  
}
```

Program

```
int a = do_something(5,  
10);  
assertEquals(a, 15);
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Test



```
int do_something(int x, int  
y) {  
    if(x < y)  
        return x+y;  
    else  
        return x*y;  
}
```

Program

```
int do_something(int x, int  
y) {  
    if(x < y)  
        return x-y;  
    else  
        return x*y;  
}
```

Mutant

```
int a = do_something(5,  
10);  
assertEquals(a, 15);
```

Test



```
int do_something(int x, int  
y) {  
    if(x < y)  
        return x+y;  
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Program

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int do_something(int x, int  
y) {  
    if(x < y)  
        return x-y;  
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Mutant

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int a = do_something(5,  
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Program

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int do_something(int x, int  
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    if(x < y)  
        return x-y;  
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        return x*y;  
}
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Mutant

```
int a = do_something(5,  
10);  
assertEquals(a, 15);
```

Test



```
int a = do_something(5,  
10);  
assertEquals(a, 15)
```

Test



# Mutants

- **Mutant**  
Slightly changed version of original program
- **Syntactic change**  
Valid (compilable code)
- **Simple**  
Programming “glitch”
- **Based on faults**  
Fault hierarchy

# Generating Mutants

- Mutation operator  
Rule to derive mutants from a program
- Mutations based on real faults  
Mutation operators represent typical errors
- Dedicated mutation operators have been defined for most languages
- For example, > 100 operators for C language

# ABS - Absolute Value Insertion

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# ABS - Absolute Value Insertion

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = abs(y);  
        y = tmp;  
    }  
  
    return x;  
}
```

# ABS - Absolute Value Insertion

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int gcd(int x, int y) {  
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    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return -abs(x);  
}
```

# ABS - Absolute Value Insertion

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int gcd(int x, int y) {  
    int tmp;  
  
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    }  
  
    return -abs(x);  
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    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return 0;  
}
```

# ABS - Absolute Value Insertion

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int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return 0;  
}
```

# AOR - Arithmetic Operator Replacement

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# AOR - Arithmetic Operator Replacement

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x * y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# AOR - Arithmetic Operator Replacement

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    }  
  
    return x;  
}
```

# AOR - Arithmetic Operator Replacement

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x * y;  
        x = y;  
        y = tmp;  
    }  
    return x;  
}
```

+,-,\*,/,%,\*\*,x,y

# ROR - Relational Operator Replacement

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# ROR - Relational Operator Replacement

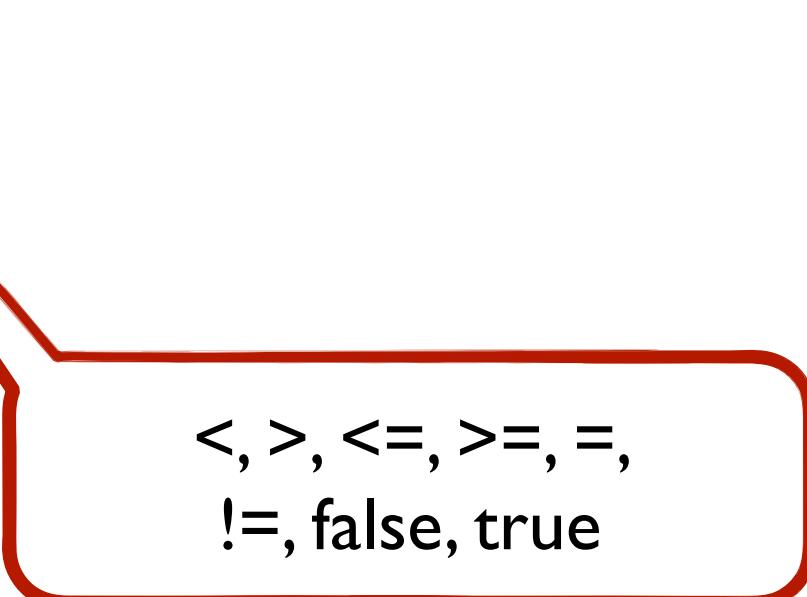
```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y > 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# ROR - Relational Operator Replacement

```
int gcd(int x, int y) {  
    int tmp;  
  
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# ROR - Relational Operator Replacement

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        x = y;  
        y = tmp;  
    }  
    return x;  
}
```



<, >, <=, >=, =,  
!=, false, true

# COR - Conditional Operator Replacement

```
if(a && b)
```

# COR - Conditional Operator Replacement

```
if(a && b)
```

```
if(a || b)
```

# COR - Conditional Operator Replacement

```
if(a && b)
```

```
if(a || b)
```

```
if(a & b)
```

# COR - Conditional Operator Replacement

```
if(a && b)
```

```
if(a || b)
```

```
if(a & b)
```

```
if(a | b)
```

# COR - Conditional Operator Replacement

```
if(a && b)
```

```
if(a || b)
```

```
if(a & b)
```

```
if(a | b)
```

```
if(a ^ b)
```

# COR - Conditional Operator Replacement

```
if(a && b)
```

```
if(a || b)
```

```
if(a & b)
```

```
if(a | b)
```

```
if(a ^ b)
```

```
if(false)
```

# COR - Conditional Operator Replacement

```
if(a && b)
```

```
if(a || b)
```

```
if(a & b)
```

```
if(a | b)
```

```
if(a ^ b)
```

```
if(false)
```

```
if(true)
```

# COR - Conditional Operator Replacement

```
if(a && b)
```

```
if(a || b)
```

```
if(a & b)
```

```
if(a | b)
```

```
if(a ^ b)
```

```
if(false)
```

```
if(true)
```

```
if(a)
```

# COR - Conditional Operator Replacement

```
if(a && b)
```

```
if(a || b)
```

```
if(a & b)
```

```
if(a | b)
```

```
if(a ^ b)
```

```
if(false)
```

```
if(true)
```

```
if(a)
```

```
if(b)
```

# SOR - Shift Operator Replacement

```
x = m << a
```

# SOR - Shift Operator Replacement

```
x = m << a
```

```
x = m >> a
```

# SOR - Shift Operator Replacement

```
x = m << a
```

```
x = m >> a
```

```
x = m >>> a
```

# SOR - Shift Operator Replacement

```
x = m << a
```

```
x = m >> a
```

```
x = m >>> a
```

```
x = m
```

# LOR - Logical Operator Replacement

```
x = m & n
```

# LOR - Logical Operator Replacement

```
x = m & n
```

```
x = m | n
```

# LOR - Logical Operator Replacement

```
x = m & n
```

```
x = m | n
```

```
x = m ^ n
```

# LOR - Logical Operator Replacement

```
x = m & n
```

```
x = m | n
```

```
x = m ^ n
```

```
x = m
```

# LOR - Logical Operator Replacement

```
x = m & n
```

x = m | n

x = m ^ n

x = m

x = n

# ASR - Assignment Operator Replacement

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# ASR - Assignment Operator Replacement

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x -= y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# ASR - Assignment Operator Replacement

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x -= y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# ASR - Assignment Operator Replacement

```
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    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
    return x;  
}
```

+ $=$ ,  $-=$ ,  $*=$ ,  $/=$ ,  $\%=$ ,  
 $\&=$ ,

# UOI - Unary Operator Insertion

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# UOI - Unary Operator Insertion

```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % +y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# UOI - Unary Operator Insertion

```
int gcd(int x, int y) {  
    int tmp;  
  
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        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# UOI - Unary Operator Insertion

```
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    int tmp;  
  
    while(y != 0) {  
        tmp = x % +y;  
        x = y;  
        y = tmp;  
    }  
    return x;  
}
```

+,-,!,<math>\sim</math>,++,--

# UOD - Unary Operator Deletion

```
if !(a > -b)
```

# UOD - Unary Operator Deletion

```
if !(a > -b)
```

```
if (a > -b)
```

# UOD - Unary Operator Deletion

```
if !(a > -b)
```

```
if (a > -b)
```

```
if !(a > b)
```

# SVR - Scalar Variable Replacement

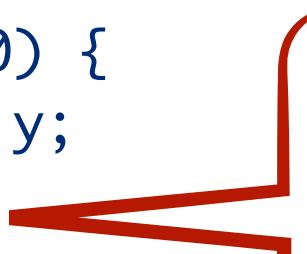
```
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = y % y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
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```

# SVR - Scalar Variable Replacement

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```

# SVR - Scalar Variable Replacement

```
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    int tmp;  
  
    while(y != 0) {  
        tmp = y % y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```



```
tmp = x % y  
tmp = x % x  
tmp = y % y  
x = x % y  
y = y % x  
tmp = tmp % y  
tmp = x % tmp
```

# OO Mutation

- So far, operators only considered method bodies
- Class level elements can be mutated as well:

# OO Mutation

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- Class level elements can be mutated as well:

```
public class test {  
    // ...  
    protected void do() {  
        // ...  
    }  
}
```

# OO Mutation

- So far, operators only considered method bodies
- Class level elements can be mutated as well:

```
public class test {  
    // ...  
    protected void do() {  
        // ...  
    }  
}
```

```
public class test {  
    // ...  
    private void do() {  
        // ...  
    }  
}
```

# OO Mutation

- AMC - Access Modifier Change
- HVD - Hiding Variable Deletion
- HVI - Hiding Variable Insertion
- OMD - Overriding Method Deletion
- OMM - Overridden Method Moving
- OMR - Overridden Method Rename
- SKR - Super Keyword Deletion
- PCD - Parent Constructor Deletion
- ATC - Actual Type Change
- DTC - Declared Type Change
- PTC - Parameter Type Change
- RTC - Reference Type Change
- OMC - Overloading Method Change
- OMD - Overloading Method Deletion
- AOC - Argument Order Change
- ANC - Argument Number Change
- TKD - this Keyword Deletion
- SMV - Static Modifier Change
- VID - Variable Initialization Deletion
- DCD - Default Constructor 2

# Interface Mutation

- Integration testing
- Change calling method by modifying the values that are sent to a called method
- Change a calling method by modifying the call
- Change a called method by modifying the values that enter/leave the method
- Change a called method by modifying statements that return from the method

# Order of Mutants

- First order mutant (FOM)  
Exactly one mutation
- Each mutation operator yields a set of FOMs
- Number of FOMs  
 $\sim$  number of data references \* number of data objects

# Order of Mutants

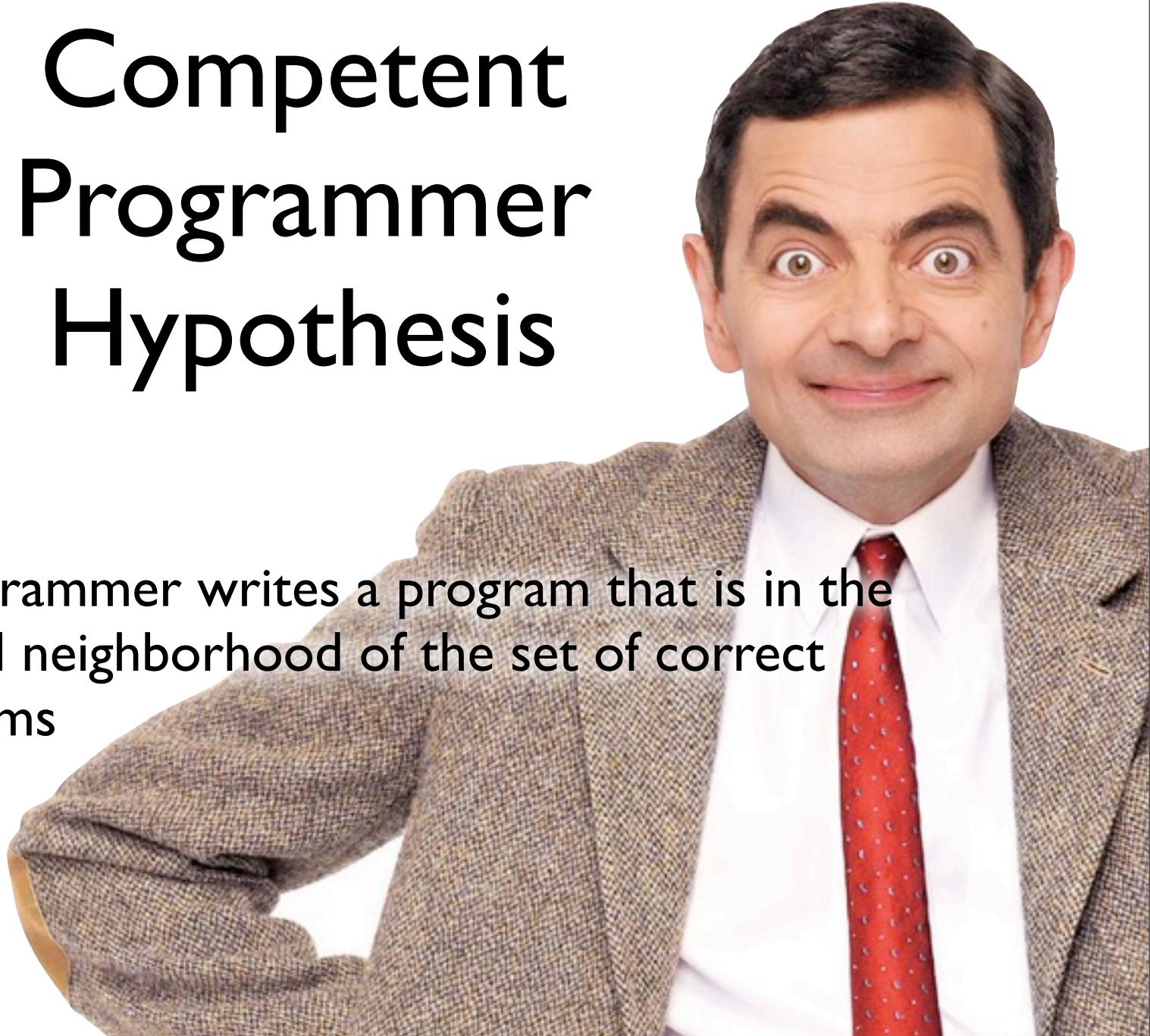
- First order mutant (FOM)  
Exactly one mutation
- Each mutation operator yields a set of FOMs
- Number of FOMs
  - ~ number of data references \* number of data objects
- Higher order mutant (HOM)  
Mutant of mutant

# Order of Mutants

- First order mutant (FOM)  
Exactly one mutation
- Each mutation operator yields a set of FOMs
- Number of FOMs
  - ~ number of data references \* number of data objects
- Higher order mutant (HOM)  
Mutant of mutant
- $\#HOM = 2^{\#FOM} - 1$

# Competent Programmer Hypothesis

A programmer writes a program that is in the general neighborhood of the set of correct programs



# Coupling Effect

Test data that distinguishes all programs differing from a correct one by only simple errors is so sensitive that it also implicitly distinguishes more complex errors.



Mutation testing focuses on  
First Order Mutants



**Competent Programmer  
Hypothesis**



**Coupling Effect**

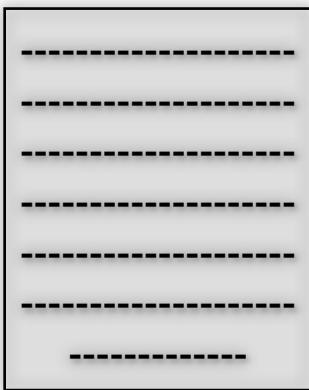
Test 1

Test 2

Test 3

Tests

## Original Program



Operators



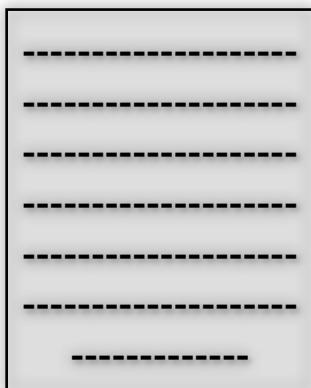
Test 1

Test 2

Test 3

Tests

Original Program



Operators



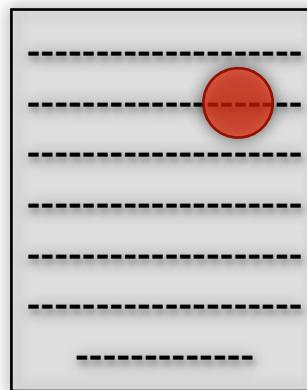
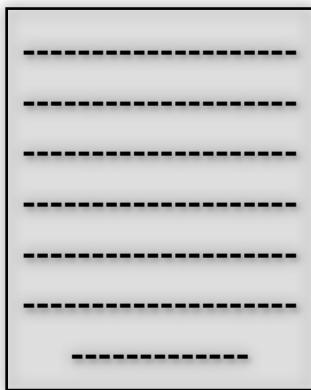
Test 1

Test 2

Test 3

Tests

Original Program



Operators



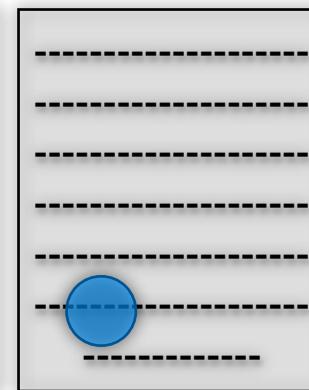
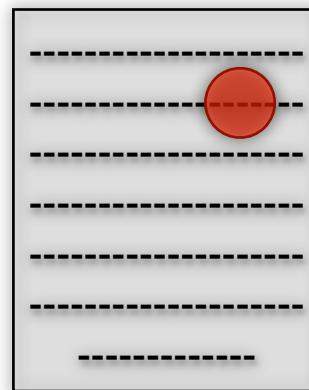
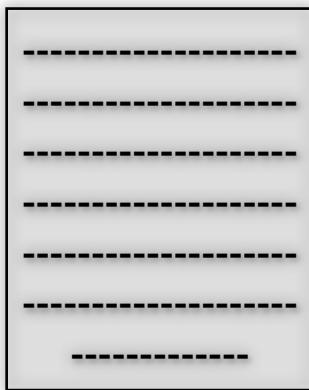
Test 1

Test 2

Test 3

Tests

Original Program



Operators



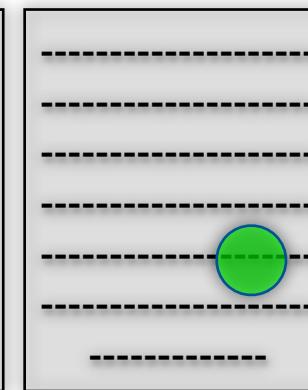
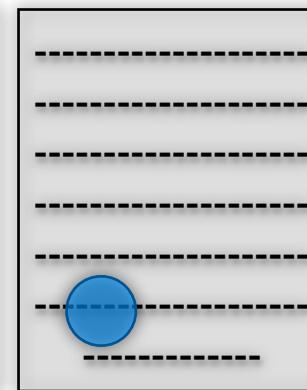
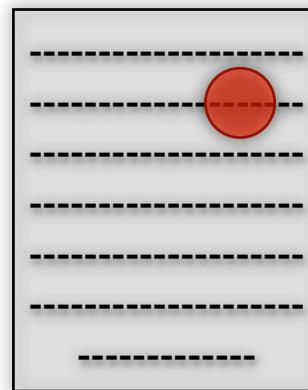
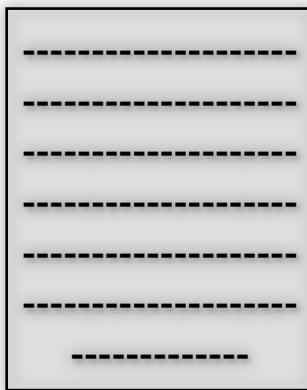
Test 1

Test 2

Test 3

Tests

Original Program



Operators



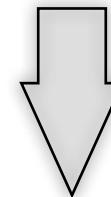
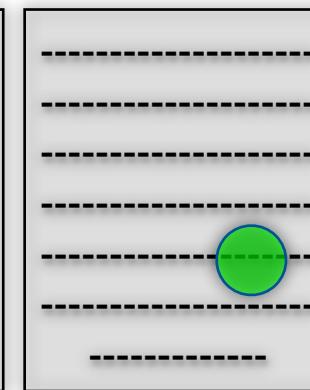
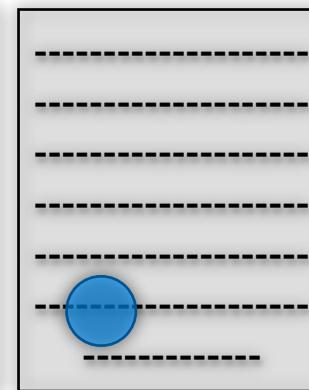
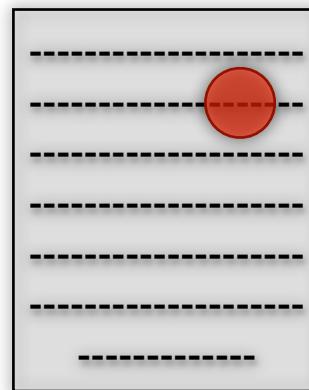
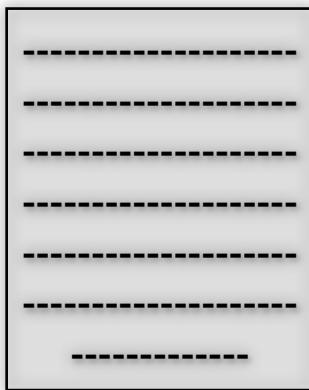
Test 1

Test 2

Test 3

Tests

Original Program



Operators



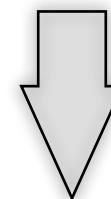
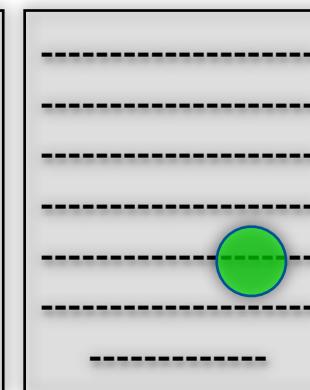
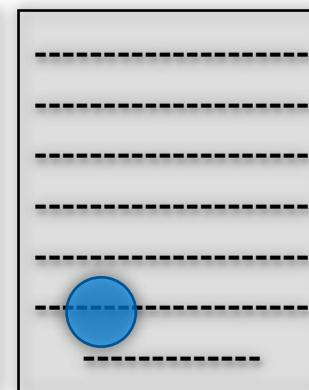
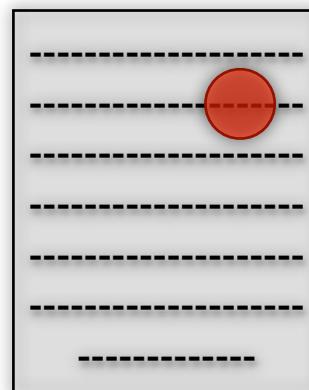
Test 1

Test 2

Test 3

Tests

Original Program



Operators



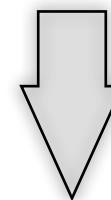
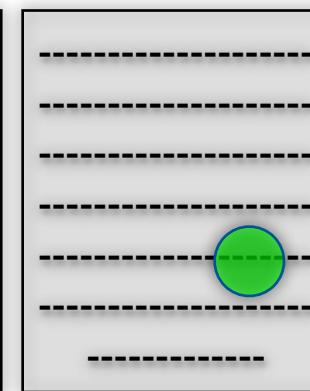
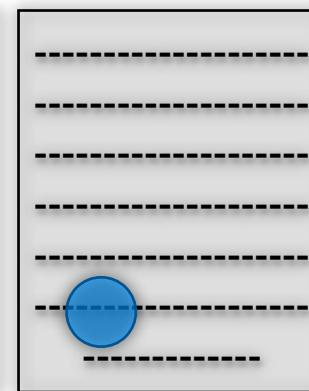
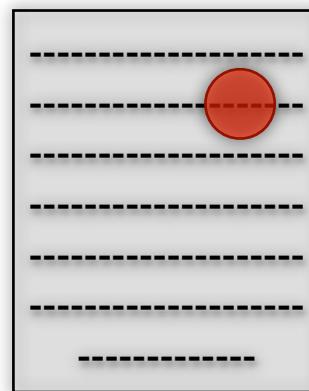
Test 1

Test 2

Test 3

Tests

Original Program



Operators



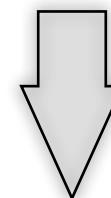
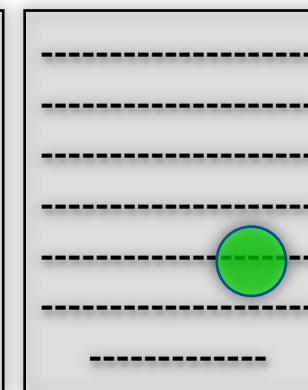
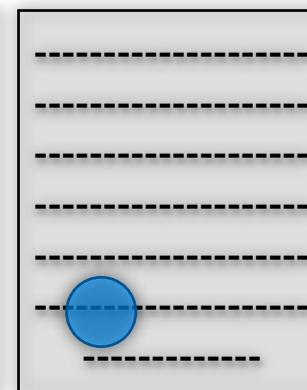
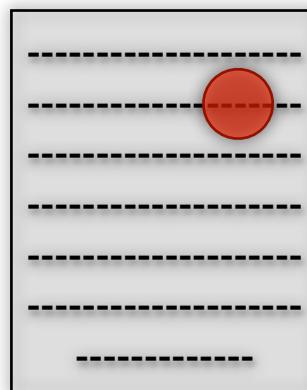
Test 1

Test 2

Test 3

Tests

Original Program



Operators



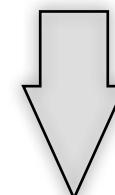
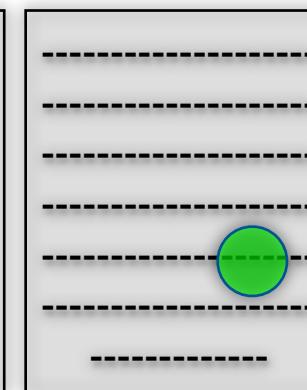
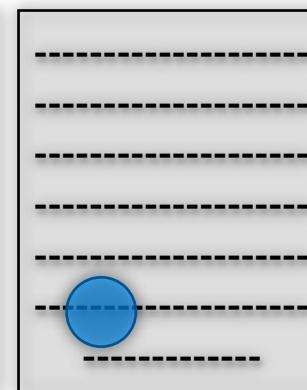
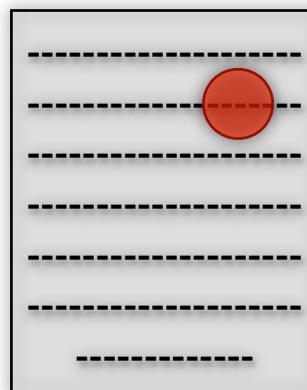
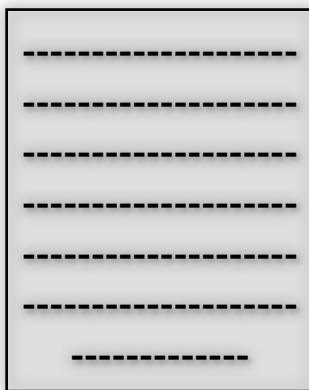
Test 1

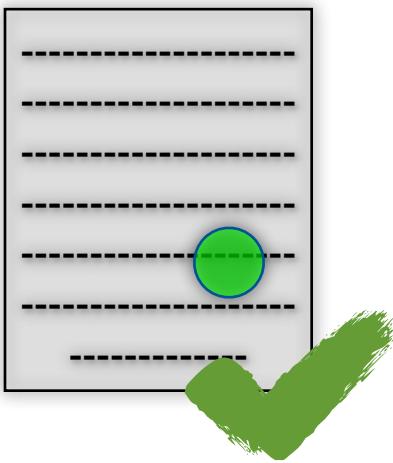
Test 2

Test 3

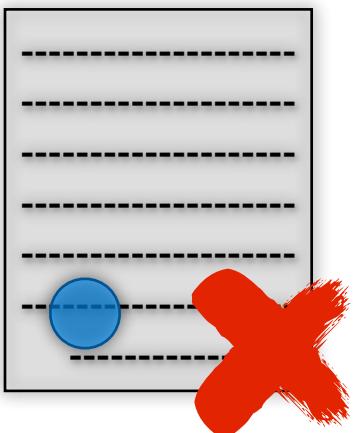
Tests

Original Program

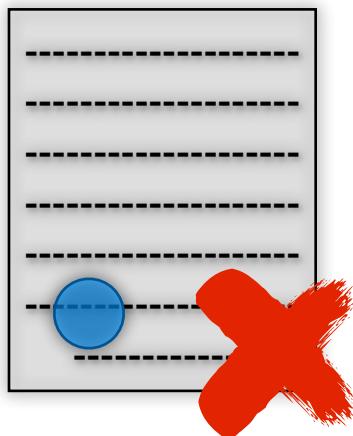
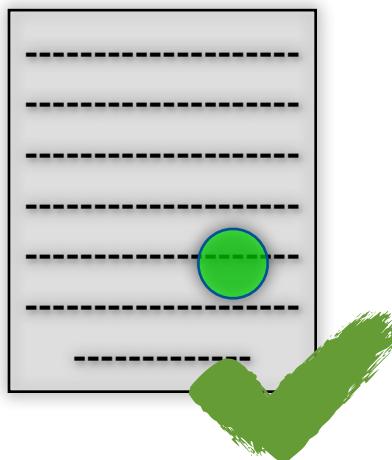




Live mutant - we need more tests



Dead mutant - of no further use

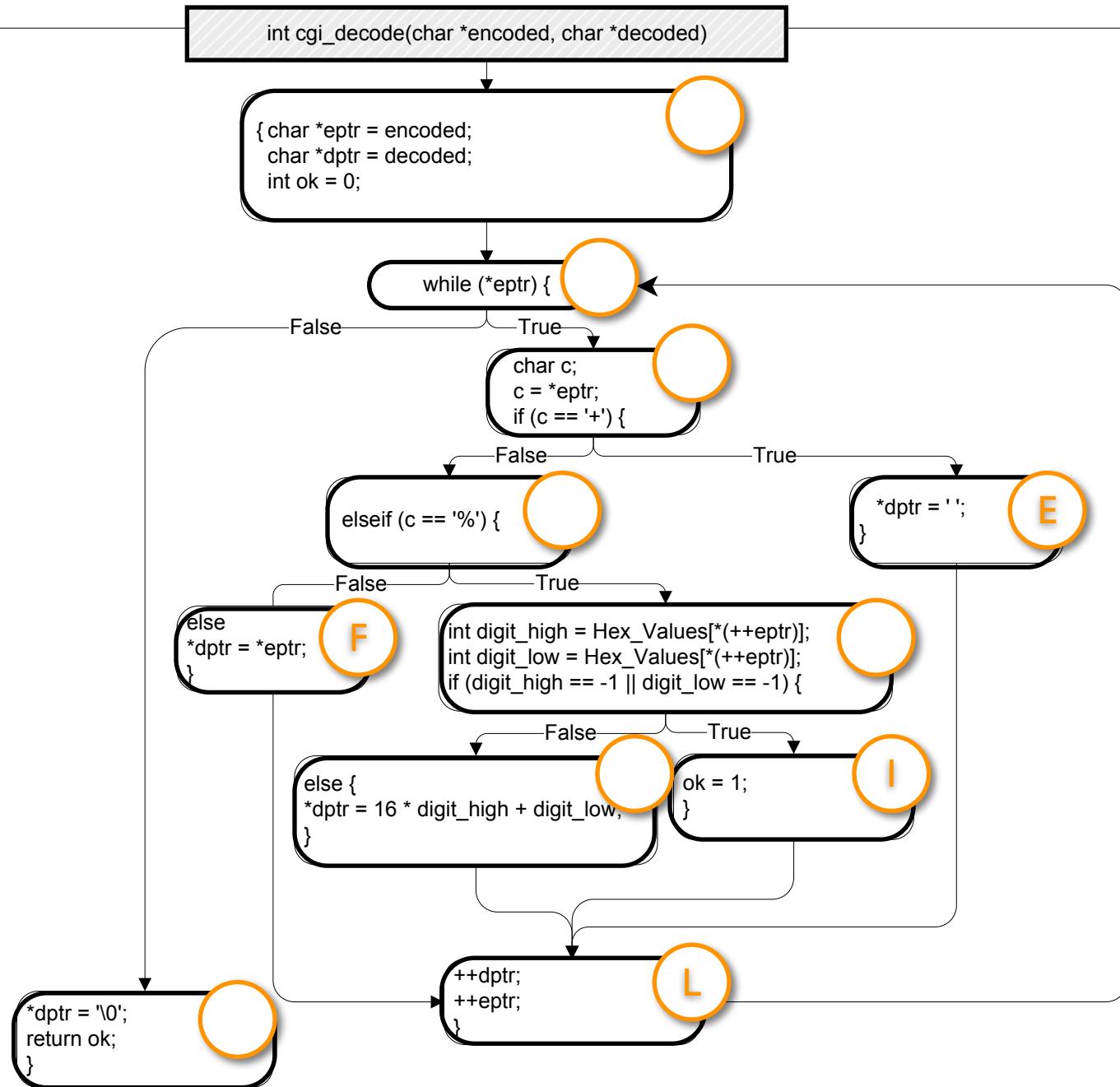


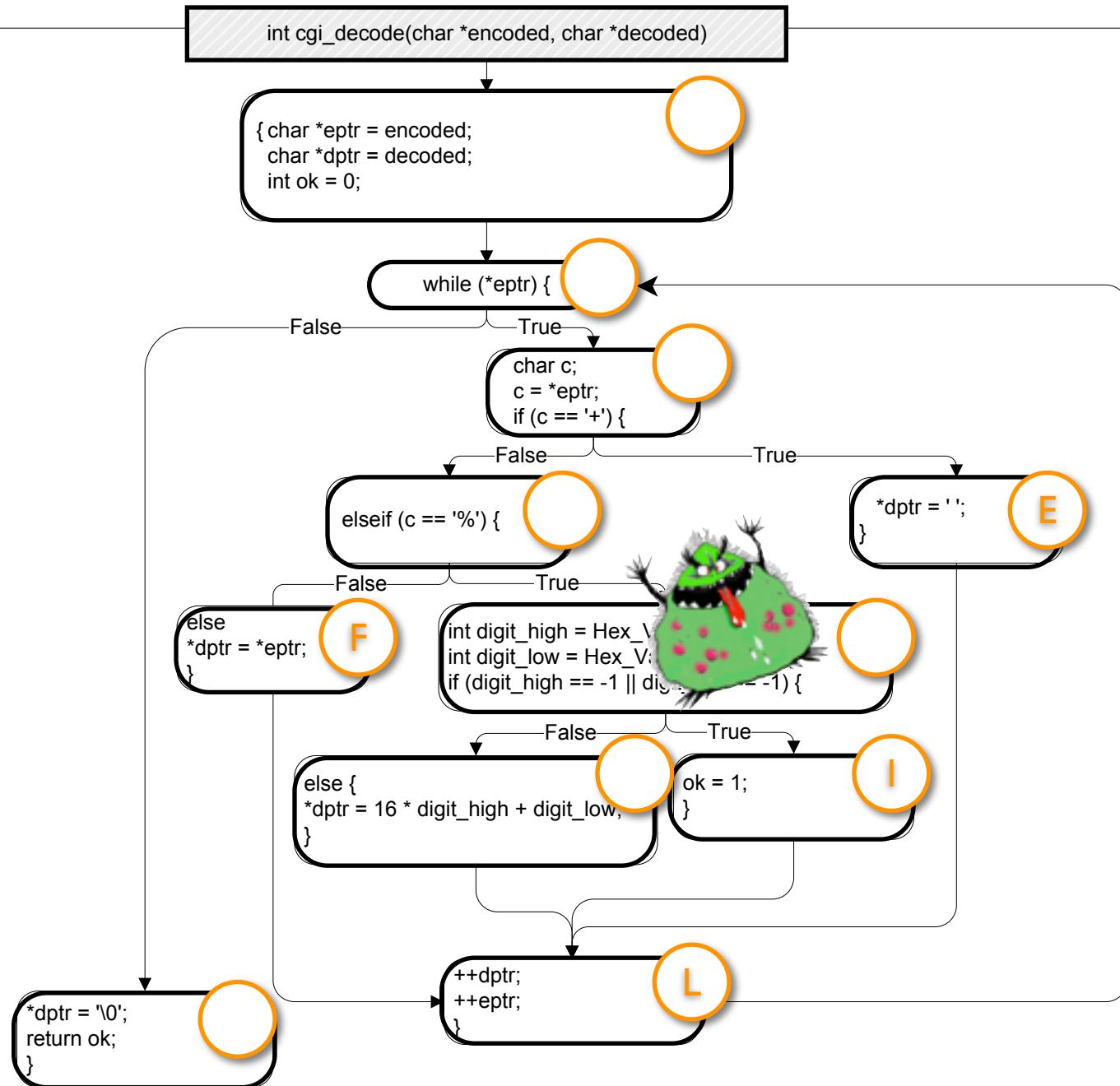
Mutation Score:

Killed Mutants

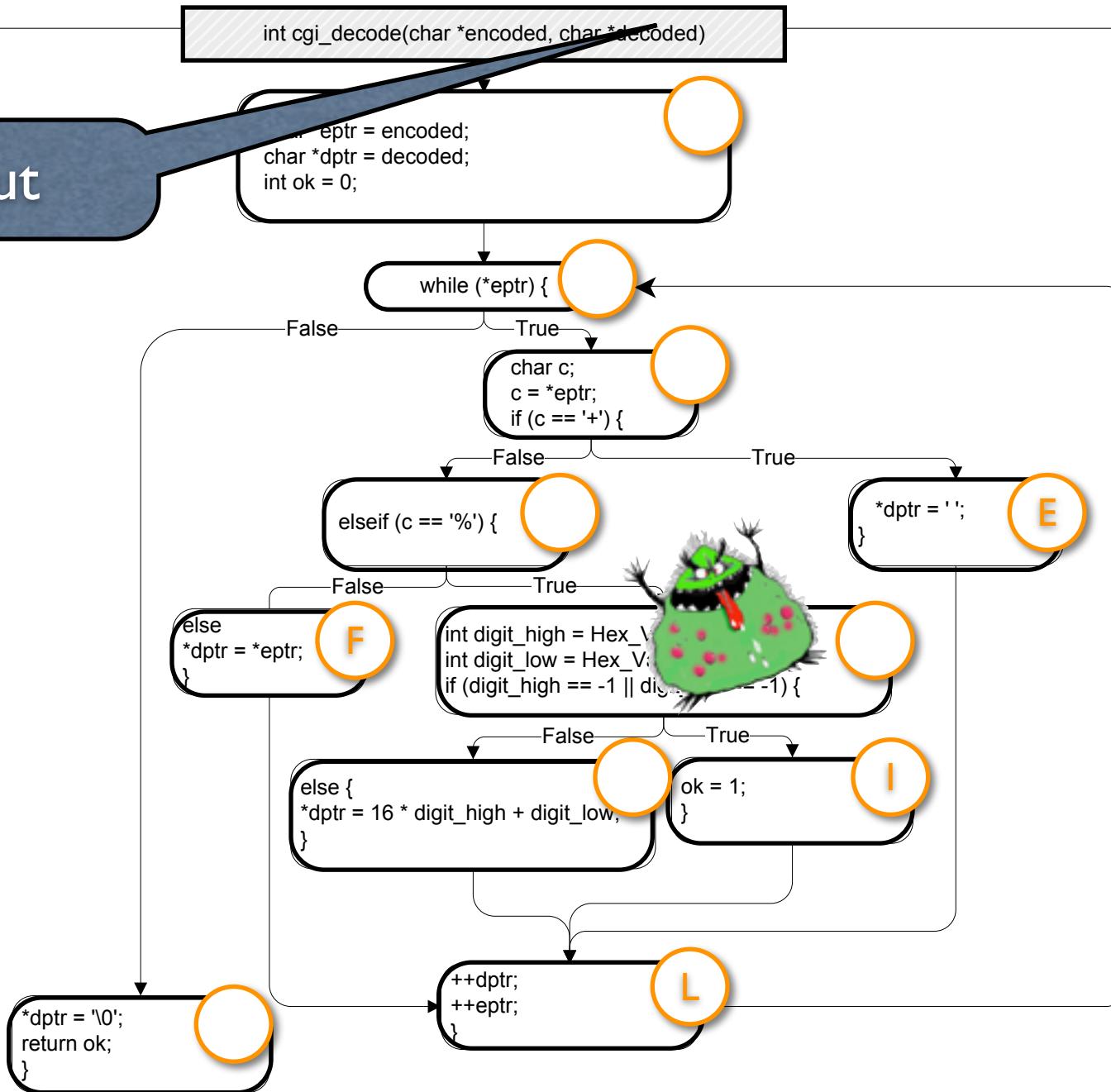
---

Total Mutants

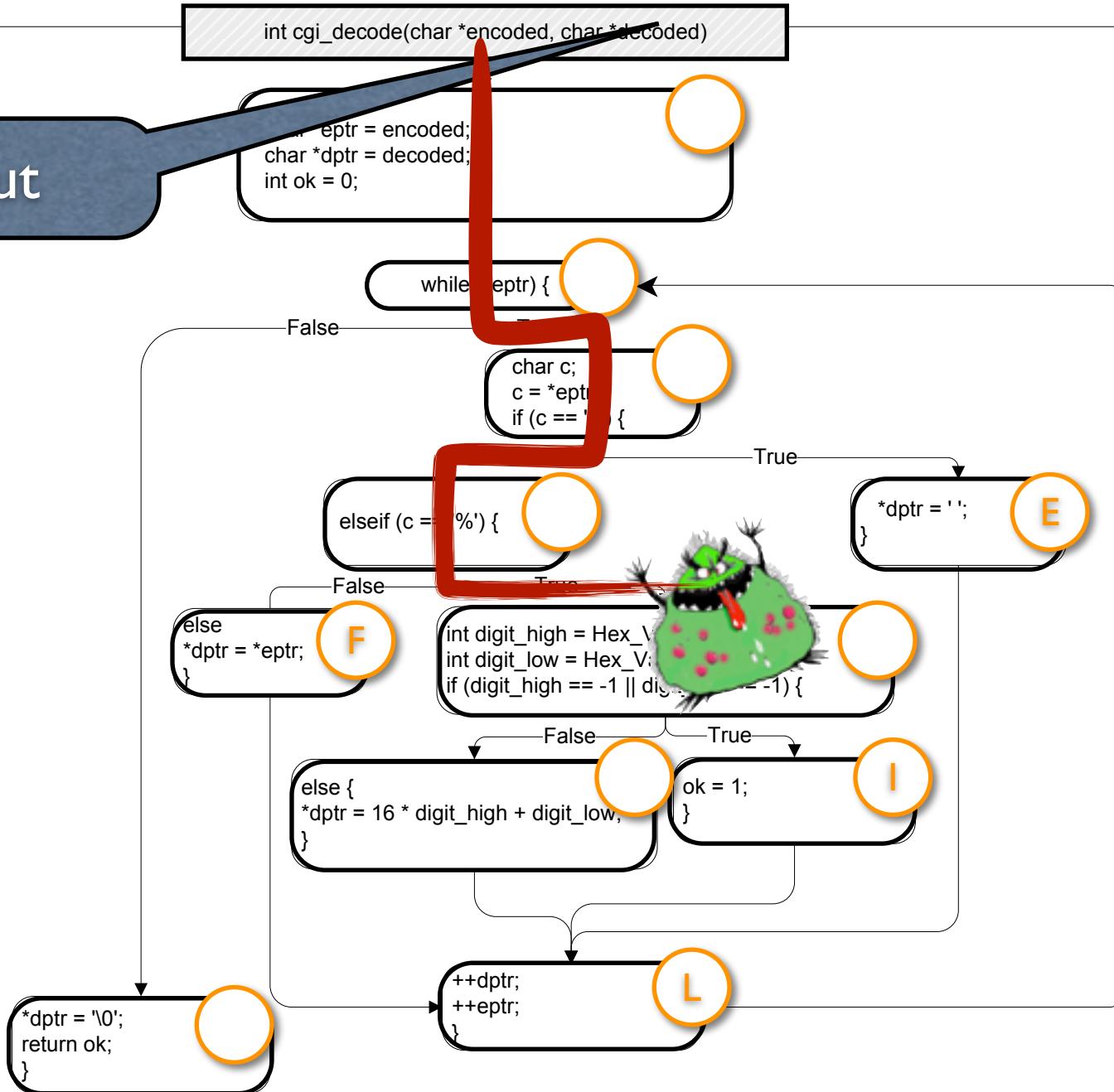




## Input



# Input



## Input

```
int cgi_decode(char *encoded, char *decoded)
```

```
    ...  
    eptr = encoded;  
    char *dptr = decoded;  
    int ok = 0;
```

```
    while (*eptr) {
```

```
        char c;  
        c = *eptr;  
        if (c == '+') {
```

```
            elseif (c == '%') {
```

```
*dptr = ' ';
```

```
E
```

```
        False
```

```
        True
```

```
        int digit_low = Hex_V;  
        if (digit_high == -1 || digit_low == -1) {
```

```
        else {
```

```
*dptr = 16 * digit_high + digit_low,  
    }
```

```
ok = 1;
```

```
I
```

```
++dptr;
```

```
++eptr;
```

```
}
```

```
L
```

## Reachability

```
*dptr = '\0';  
return ok;  
}
```

## Input

```
int cgi_decode(char *encoded, char *decoded)
```

```
    ...  
    eptr = encoded;  
    char *dptr = decoded;  
    int ok = 0;
```

```
    while (*eptr) {
```

```
        char c;  
        c = *eptr;  
        if (c == '+') {
```

```
            elseif (c == '%') {
```

```
                *dptr = ' ';
```

```
E
```

```
        False
```

```
        True
```

```
        int digit_low = Hex_V;  
        if (digit_high == -1 || digit_low == -1) {
```

```
        else {  
            *dptr = 16 * digit_high + digit_low,  
        }
```

```
ok = 1;
```

## Infection

## Reachability

```
*dptr = '\0';  
return ok;  
}
```

```
L
```

```
++dptr;  
++eptr;  
}
```

## Input

```
int cgi_decode(char *encoded, char *decoded)
```

```
    ...  
    eptr = encoded;  
    char *dptr = decoded;  
    int ok = 0;
```

```
    while (*eptr) {
```

False

```
        char c;  
        c = *eptr;  
        if (c == '+') {
```

True

```
            elseif (c == '%') {
```

False

```
                int digit_low = Hex_V;  
                if (digit_high == -1 || digit_low == -1) {
```

```
*dptr = ' ';
```

E

True

```
            else {  
                *dptr = 16 * digit_high + digit_low,  
            }
```

```
ok = 1;
```

## Infection

```
            ++dptr;  
            ++eptr;  
        }
```

## Reachability

```
*dptr = '\0';  
return ok;  
}
```

## Input

```
int cgi_decode(char *encoded, char *decoded)
```

```
    ...  
    eptr = encoded;  
    char *dptr = decoded;  
    int ok = 0;
```

## Reachability

## Propagation

## Infection

```
*dptr = '\0';  
return ok;  
}
```

```
while (*eptr) {
```

False

```
char c;  
c = *eptr;  
if (c == '+') {
```

True

```
elseif (c == '%') {
```

False

```
    int digit_low = Hex_V;  
    if (digit_high == -1 || digit_low == -1) {
```

```
*dptr = ' ';
```

E

True

```
else {  
    *dptr = 16 * digit_high + digit_low,  
}
```

```
ok = 1;
```

I

True

```
++dptr;  
++eptr;
```

L

# Equivalent Mutants

- Mutation = syntactic change
- The change might leave the semantics unchanged
- Equivalent mutants are hard to detect  
(undecidable problem)
- Might be reached, but no infection
- Might infect, but no propagation

# Example 1

```
int max(int[] values) {  
    int r, i;  
  
    r = 0;  
    for(i = 1; i<values.length; i++) {  
        if (values[i] > values[r])  
            r = i;  
    }  
  
    return values[r];  
}
```

# Example I

```
int max(int[] values) {  
    int r, i;  
  
    r = 0;  
    for(i = 0; i<values.length; i++) {  
        if (values[i] > values[r])  
            r = i;  
    }  
  
    return values[r];  
}
```

# Example I

```
int max(int[] values) {  
    int r, i;  
  
    r = 0;  
    for(i = 0; i<values.length; i++) {  
        if (values[i] > values[r])  
            r = i;  
    }  
  
    return values[r];  
}
```

# Example I

```
int max(int[] values) {  
    int r, i;  
  
    r = 0;  
    for(i = 1; i<values.length; i++) {  
        if (values[i] >= values[r])  
            r = i;  
    }  
  
    return values[r];  
}
```

# Example I

```
int max(int[] values) {  
    int r, i;  
  
    r = 0;  
    for(i = 1; i<values.length; i++) {  
        if (values[i] >= values[r])  
            r = i;  
    }  
  
    return values[r];  
}
```

# Example I

```
int max(int[] values) {  
    int r, i;  
  
    r = 0;  
    for(i = 1; i<values.length; i++) {  
        if (values[r] > values[i])  
            r = i;  
    }  
  
    return values[r];  
}
```

# Example I

```
int max(int[] values) {  
    int r, i;  
  
    r = 0;  
    for(i = 1; i<values.length; i++) {  
        if (values[r] > values[i])  
            r = i;  
    }  
  
    return values[r];  
}
```

# Example 2

```
if(x > 0) {  
    if(y > x) {  
        // ...  
    }  
}
```

# Example 2

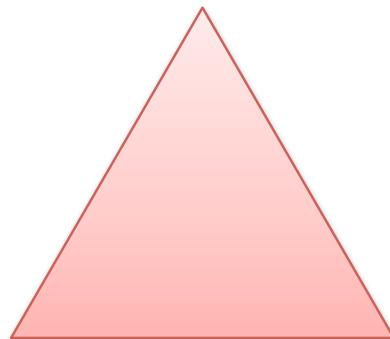
```
if(x > 0) {  
    if(y > abs(x)) {  
        // ...  
    }  
}
```

# Example 2

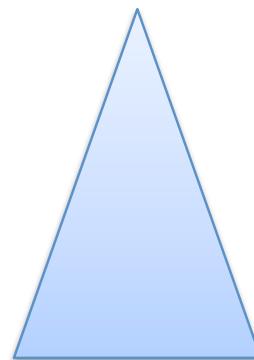
```
if(x > 0) {  
    if(y > abs(x)) {  
        // ...  
    }  
}
```

# Example

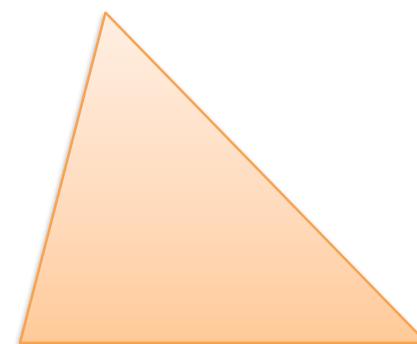
Classify triangle by the length of the sides



Equilateral



Isosceles



Scalene

```
int triangle(int a, int b, int c) {  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
  
    return 3; // scalene  
}
```

```
int triangle(int a, int b, int c) {  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
  
    return 3; // scalene  
}
```



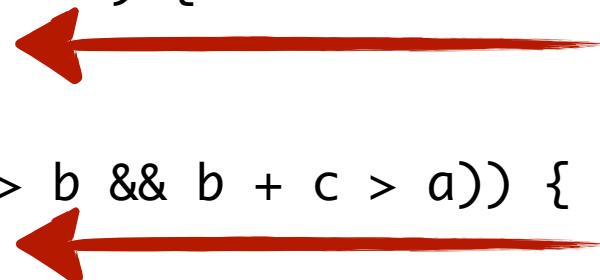
```
int triangle(int a, int b, int c) {  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
  
    return 3; // scalene  
}
```



(0, 0, 0)

```
int triangle(int a, int b, int c) {  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
  
    return 3; // scalene  
}
```

(0, 0, 0)



```
int triangle(int a, int b, int c) {  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
  
    return 3; // scalene  
}
```

(0, 0, 0)

(1, 1, 3)

```
int triangle(int a, int b, int c) {  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
  
    return 3; // scalene  
}
```

(0, 0, 0)

(1, 1, 3)

```
int triangle(int a, int b, int c) {  
  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid ← (0, 0, 0)  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid ← (1, 1, 3)  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral ← (2, 2, 2)  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
  
    return 3; // scalene  
}
```

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

```
int triangle(int a, int b, int c) {  
  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid ← (0, 0, 0)  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid ← (1, 1, 3)  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral ← (2, 2, 2)  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles ←  
    }  
  
    return 3; // scalene  
}
```

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

```
int triangle(int a, int b, int c) {
```

```
    if (a <= 0 || b <= 0 || c <= 0) {
```

```
        return 4; // invalid
```

```
}
```

```
    if (!(a + b > c && a + c > b && b + c > a)) {
```

```
        return 4; // invalid
```

```
}
```

```
    if (a == b && b == c) {
```

```
        return 1; // equilateral
```

```
}
```

```
    if (a == b || b == c || a == c) {
```

```
        return 2; // isosceles
```

```
}
```

```
    return 3; // scalene
```

```
}
```

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

(2, 2, 3)

```
int triangle(int a, int b, int c) {  
  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid ← (0, 0, 0)  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid ← (1, 1, 3)  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral ← (2, 2, 2)  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles ← (2, 2, 3)  
    }  
  
    return 3; // scalene ← (3, 3, 3)  
}
```

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

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```
int triangle(int a, int b, int c) {  
  
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        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

(0, 0, 0)  
(1, 1, 3)  
(2, 2, 2)  
(2, 2, 3)  
(2, 3, 4)

```
int triangle(int a, int b, int c) {  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a++ == c) {  
        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

(0, 0, 0)  
(1, 1, 3)  
(2, 2, 2)  
(2, 2, 3)  
(2, 3, 4)

```
int triangle(int a, int b, int c) {  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a++ == c) {  
        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

(2, 2, 3)

(2, 3, 4)

```
int triangle(int a, int b, int c) {  
  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
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    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a++ == c) {  
        return 2; // isosceles  
    }  
  
    return 3; // scalene  
}
```

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

(2, 2, 3)

(2, 3, 4)

```
int triangle(int a, int b, int c) {  
  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
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    if (a == b || b == c || a++ == c) {  
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    }  
  
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}
```

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

(2, 2, 3)

(2, 3, 4)



```
int triangle(int a, int b, int c) {  
  
    if (a <= 0 || b <= 0 || c <= 0) {  
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        return 1; // equilateral  
    }  
    if (a == b || b == c || a++ == c) {  
        return 2; // isosceles  
    }  
  
    return 3; // scalene  
}
```

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

(2, 2, 3)

(2, 3, 4)



```

int triangle(int a, int b, int c) {

    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
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    }
    if (a == b && b == c) {
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    if (a == b || b == c || a++ == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

(2, 2, 3)

(2, 3, 4)



```
int triangle(int a, int b, int c) {  
    if (b <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
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    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

(0, 0, 0)



(1, 1, 3)



(2, 2, 2)



(2, 2, 3)



(2, 3, 4)



```
int triangle(int a, int b, int c) {  
    if (b <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

(0, 0, 0)



(1, 1, 3)



(2, 2, 2)



(2, 2, 3)



(2, 3, 4)



```
int triangle(int a, int b, int c) {  
    if (b <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

(0, 1, 1)

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

(2, 2, 3)

(2, 3, 4)

```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 1, 1)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a >= c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 0, 0) 

(1, 1, 3) 

(2, 2, 2) 

(2, 2, 3) 

(2, 3, 4) 

```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 1, 1)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a >= c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(4, 3, 2)

(0, 0, 0)



(1, 1, 3)



(2, 2, 2)



(2, 2, 3)



(2, 3, 4)



```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 1, 1)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
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    }
    if (a == b || b == c || a >= c) {
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    }

    return 3; // scalene
}

```

(4, 3, 2)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a * b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

(2, 2, 3)

(2, 3, 4)

```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 1, 1)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a >= c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(4, 3, 2)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
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        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(1, 1, 1)

(0, 0, 0)

(1, 1, 3)

(2, 2, 2)

(2, 2, 3)

(2, 3, 4)

```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 1, 1)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a >= c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(4, 3, 2)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a * b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(1, 1, 1)

```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c++) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 0, 0)



(1, 1, 3)



(2, 2, 2)



(2, 2, 3)



(2, 3, 4)



```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 1, 1)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a >= c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(4, 3, 2)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a * b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(1, 1, 1)

```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c++) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(2, 3, 2)

(0, 0, 0)



(1, 1, 3)



(2, 2, 2)



(2, 2, 3)



(2, 3, 4)



```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(0, 1, 1)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
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    }
    if (a == b || b == c || a >= c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(4, 3, 2)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a * b > c && a + c > b && b + c > a)) {
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    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(1, 1, 1)

```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c++) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }

    return 3; // scalene
}

```

(2, 3, 2)

(0, 0, 0)



(1, 1, 3)



(2, 2, 2)



(2, 2, 3)



(2, 3, 4)



```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c) {
        return 2; // isosceles
    }
    return 3; // scalene
}

```

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a * b > c && a * c > b && b * c > a)) {
        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }
    return 3; // scalene
}

```

(1, 1, 1)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
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    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }
    return 3; // scalene
}

```

(2, 3, 2)

- (0, 0, 0) 
- (1, 1, 3) 
- (2, 2, 2) 
- (2, 2, 3) 
- (2, 3, 4) 

```

int triangle(int a, int b, int c) {
    if (b <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a + b > c && a + c > b && b + c > a)) {
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    }
    if (a == b && b == c) {
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    }
    if (a == b || b == c) {
        return 2; // isosceles
    }
    return 3; // scalene
}

```

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
    if (!(a * b > c && a * c > b && b * c > a)) {
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    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }
    return 3; // scalene
}

```

(1, 1, 1)

```

int triangle(int a, int b, int c) {
    if (a <= 0 || b <= 0 || c <= 0) {
        return 4; // invalid
    }
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        return 4; // invalid
    }
    if (a == b && b == c) {
        return 1; // equilateral
    }
    if (a == b || b == c || a == c) {
        return 2; // isosceles
    }
    return 3; // scalene
}

```

(2, 3, 2)

- (0, 0, 0) 
- (1, 1, 3) 
- (2, 2, 2) 
- (2, 2, 3) 
- (2, 3, 4) 

equivalent!

# Performance



```
int triangle(int a, int b, int c) {  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

$$a + b > c$$

# $a + b > c$

|                          |                |                 |
|--------------------------|----------------|-----------------|
| $a - b > c$              | $a - b \geq c$ | $a - b > 0$     |
| $a * b > c$              | $a - b < c$    | $++a - b > c$   |
| $a / b > c$              | $a - b \leq c$ | $a - ++b > c$   |
| $a \% b > c$             | $a - b = c$    | $a - b > ++c$   |
| $a > c$                  | $a - b != c$   | $--a - b > c$   |
| $b > c$                  | $b - b > c$    | $a - --b > c$   |
| $\text{abs}(a) - b > c$  | $a - a > c$    | $a - b > --c$   |
| $a - \text{abs}(b) > c$  | $c - b > c$    | $++(a - b) > c$ |
| $a - b > \text{abs}(c)$  | $a - c > c$    | $--(a - b) > c$ |
| $\text{abs}(a - b) > c$  | $a - b > a$    | $-a - b > c$    |
| $-\text{abs}(a) - b > c$ | $a - b > b$    | $a - -b > c$    |
| $a - -\text{abs}(b) > c$ | $a - b > c$    | $a - b > -c$    |
| $a - b > -\text{abs}(c)$ | $0 - b > c$    | $-(a - b) > c$  |
| $-\text{abs}(a - b) > c$ | $a - 0 > c$    | $0 > c$         |

# Performance Problems

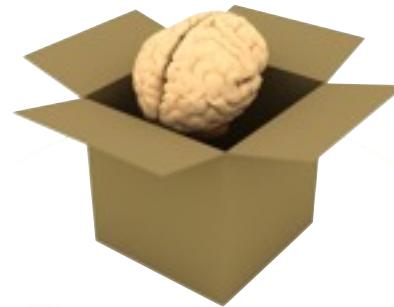
- Many mutation operators possible  
Proteum - 103 Mutation Operators for C  
MuJava - Adds 24 Class level Mutation Operators
- Each mutation operator results in many mutants  
Depending on program under test
- Each mutant needs to be compiled
- Each test case needs to be executed against every mutant



# Improvements



Do fewer



Do smarter



Do faster

- Mutant sampling
- Selective mutation
- Parallelize
- Weak mutation
- Use coverage
- Impact
- Mutate bytecode
- Mutant schemata

# Using Coverage

```
int triangle(int a, int b, int c) {  
  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

(0, 0, 0)  
(1, 1, 3)  
(2, 2, 2)  
(2, 2, 3)  
(2, 3, 4)  
(0, 1, 1)  
(4, 3, 2)  
(1, 1, 1)  
(2, 3, 2)

# Using Coverage

```
int triangle(int a, int b, int c) {  
  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a)) {  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

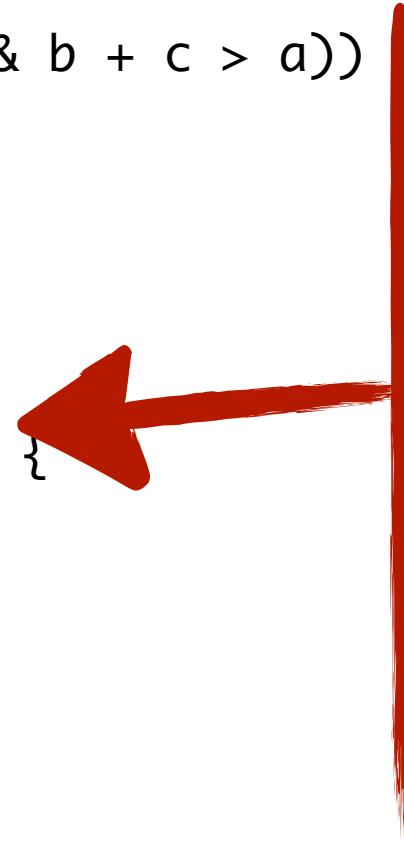
(0, 0, 0)  
(1, 1, 3)  
(2, 2, 2)  
(2, 2, 3)  
(2, 3, 4)  
(0, 1, 1)  
(4, 3, 2)  
(1, 1, 1)  
(2, 3, 2)



# Using Coverage

```
int triangle(int a, int b, int c) {  
  
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    if (!(a + b > c && a + c > b && b + c > a))  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

- (0, 0, 0)
- (1, 1, 3)
- (2, 2, 2)
- (2, 2, 3) 
- (2, 3, 4) 
- (0, 1, 1)
- (4, 3, 2) 
- (1, 1, 1)
- (2, 3, 2) 



# Using Coverage

```
int triangle(int a, int b, int c) {  
  
    if (a <= 0 || b <= 0 || c <= 0) {  
        return 4; // invalid  
    }  
    if (!(a + b > c && a + c > b && b + c > a))  
        return 4; // invalid  
    }  
    if (a == b && b == c) {  
        return 1; // equilateral  
    }  
    if (a == b || b == c || a == c) {  
        return 2; // isosceles  
    }  
    return 3; // scalene  
}
```

Only these tests execute mutants in this line!

- (0, 0, 0)
- (1, 1, 3)
- (2, 2, 2)
- (2, 2, 3) (circled)
- (2, 3, 4) (circled)
- (0, 1, 1)
- (4, 3, 2) (circled)
- (1, 1, 1)
- (2, 3, 2) (circled)

# Strong vs. Weak Mutation

- Strong mutation  
Mutation has propagated to some observable behavior
- Weak mutation  
Mutation has affected state (infection)
- Compare internal state after mutation
- Does not guarantee propagation
- Reported to save 50% execution time



# Strong vs. Weak Mutation

```
int gcd(int x, int y) {      int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}  
  
int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x * y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

# Strong vs. Weak Mutation

```
int gcd(int x, int y) {      int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}  
  
int gcd(int x, int y) {      int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x * y;  
        x = y;  
        y = tmp;  
    }  
  
    return x;  
}
```

Strong mutation

# Strong vs. Weak Mutation

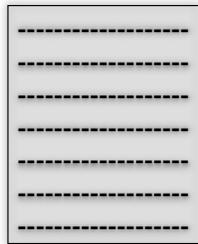
```
int gcd(int x, int y) {      int gcd(int x, int y) {  
    int tmp;  
  
    while(y != 0) {  
        tmp = x % y;  ← Weak mutation →  
        x = y;  
        y = tmp;  
    }  
  
    return x;  ← Strong mutation →  
}
```

The diagram illustrates two versions of the Euclidean algorithm for calculating the greatest common divisor (GCD). The left version is labeled "Weak mutation" and the right version is labeled "Strong mutation".

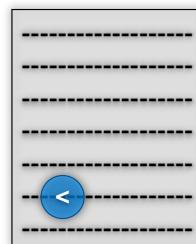
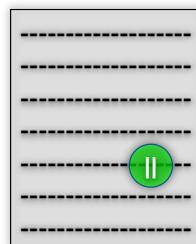
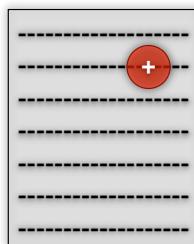
- Weak mutation:** This version uses the modulus operator (%). It iterates until y is 0, updating x to y and y to tmp in each iteration.
- Strong mutation:** This version uses multiplication (\*). It iterates until y is 0, updating tmp to x \* y, x to y, and y to tmp in each iteration.

Both versions end with a return statement that returns the value of x.

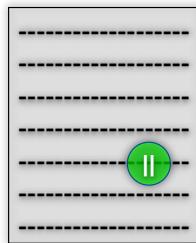
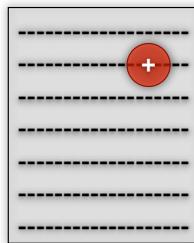
# Mutant Schemata



# Mutant Schemata

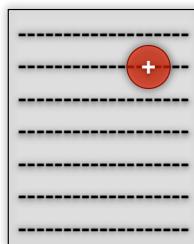
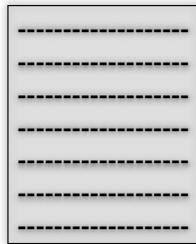


# Mutant Schemata

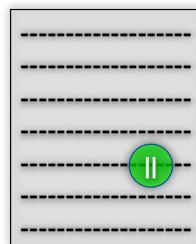


Mutant I:  
Compile  
Execute

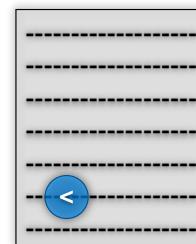
# Mutant Schemata



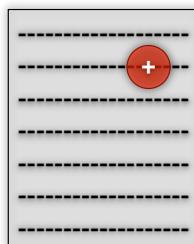
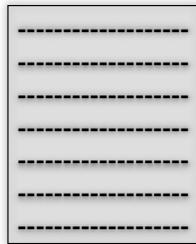
Mutant 1:  
Compile  
Execute



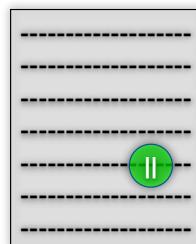
Mutant 2:  
Compile  
Execute



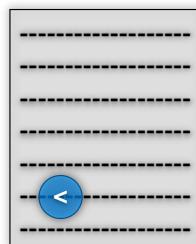
# Mutant Schemata



Mutant 1:  
Compile  
Execute

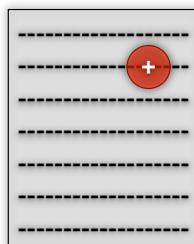


Mutant 2:  
Compile  
Execute

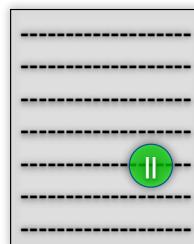


Mutant 3:  
Compile  
Execute

# Mutant Schemata



Mutant 1:  
Compile  
Execute

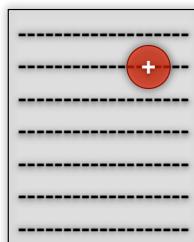


Mutant 2:  
Compile  
Execute

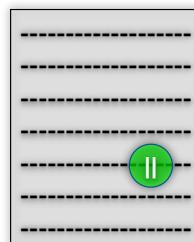


Mutant 3:  
Compile  
Execute

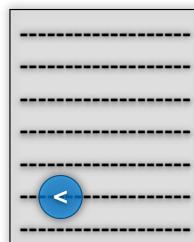
# Mutant Schemata



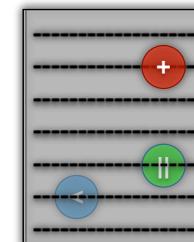
Mutant 1:  
Compile  
Execute



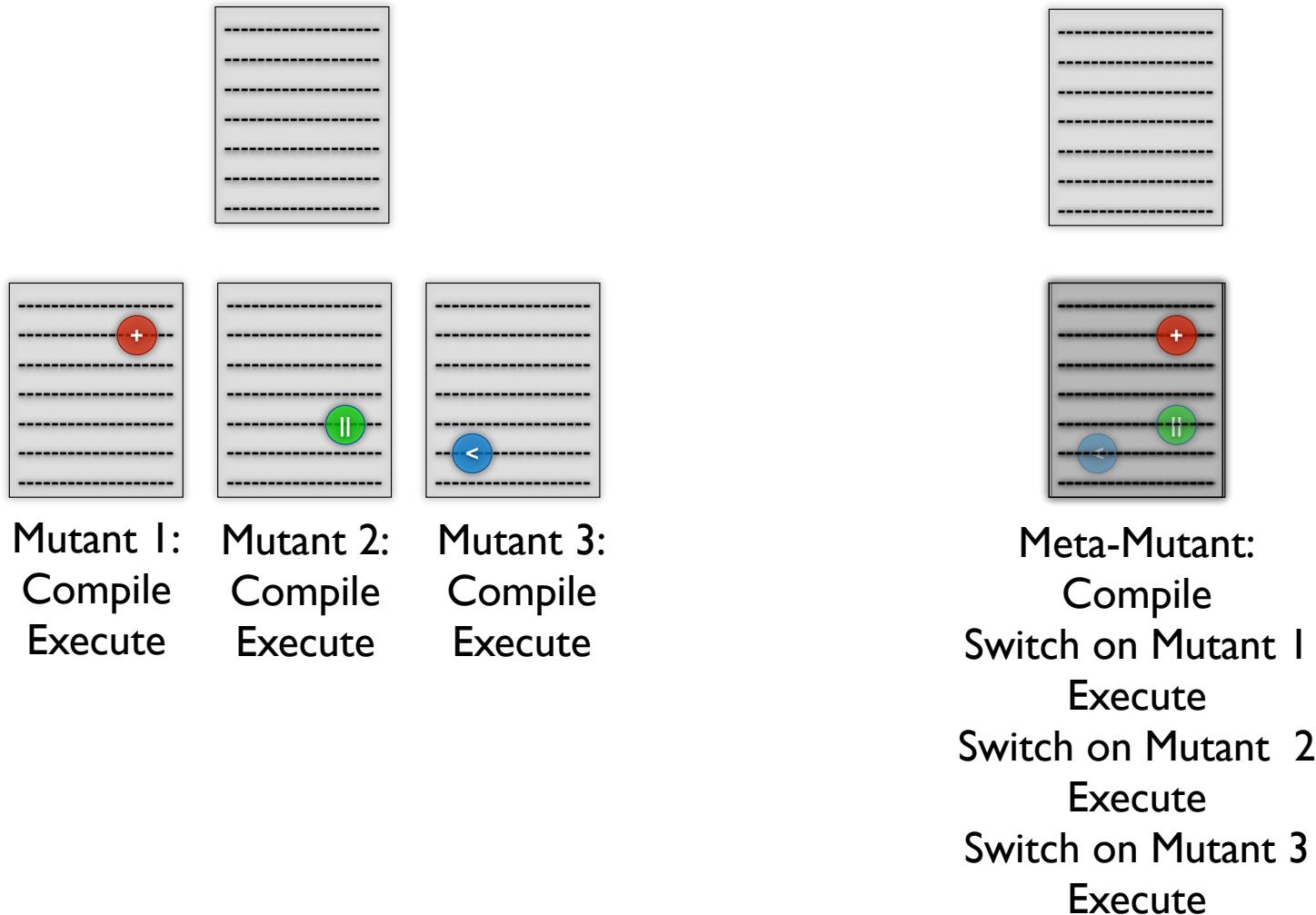
Mutant 2:  
Compile  
Execute



Mutant 3:  
Compile  
Execute



# Mutant Schemata

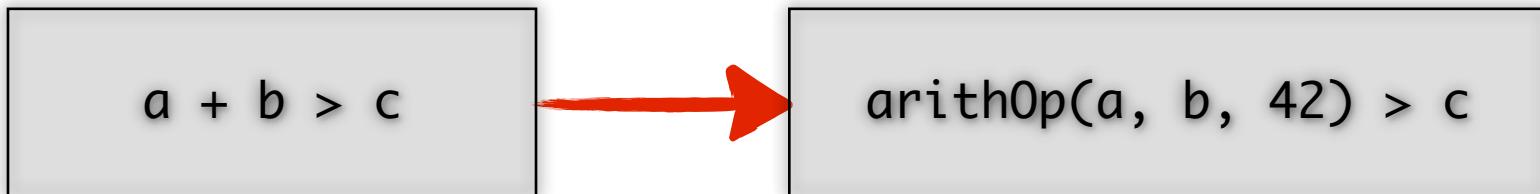


# Mutant Schemata

$a + b > c$

`arithOp(a, b, 42) > c`

# Mutant Schemata



# Mutant Schemata

$a + b > c$

`arithOp(a, b, 42) > c`

```
int arithOp(int op1, int op2, int location) {  
    switch(variant(location)) {  
        case aoADD:    return op1 + op2;  
        case aoSUB:    return op1 - op2;  
        case aoMULT:   return op1 * op2;  
        case aoDIV:    return op1 / op2;  
        case aoMOD:    return op1 % op2;  
        case aoLEFT:   return op1;  
        case aoRIGHT:  return op2;  
    }  
}
```

# Mutant Schemata

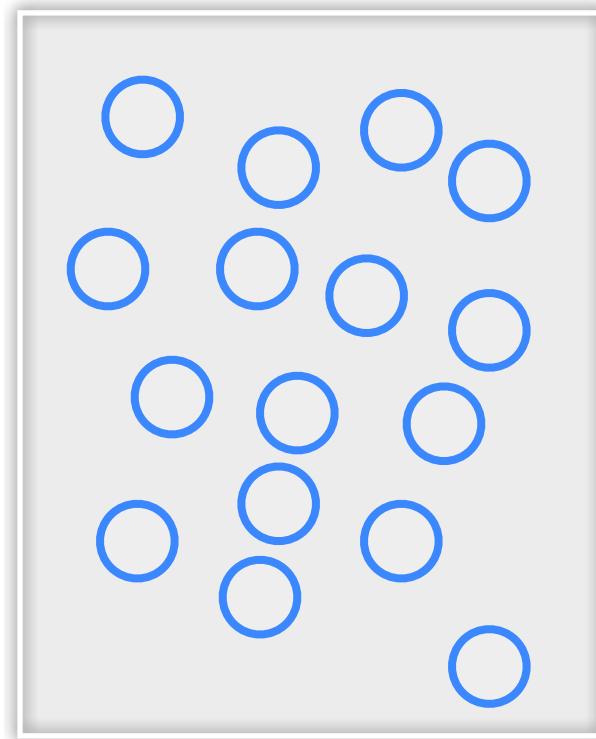
$a + b > c$

`arithOp(a, b, 42) > c`

```
int arithOp(int op1, int op2, int location) {  
    switch(variant(location)) {  
        case aoADD:    return op1 + op2;  
        case aoSUB:    return op1 - op2;  
        case aoMULT:   return op1 * op2;  
        case aoDIV:    return op1 / op2;  
        case aoMOD:    return op1 % op2;  
        case aoLEFT:   return op1;  
        case aoRIGHT:  return op2;  
    }  
}
```

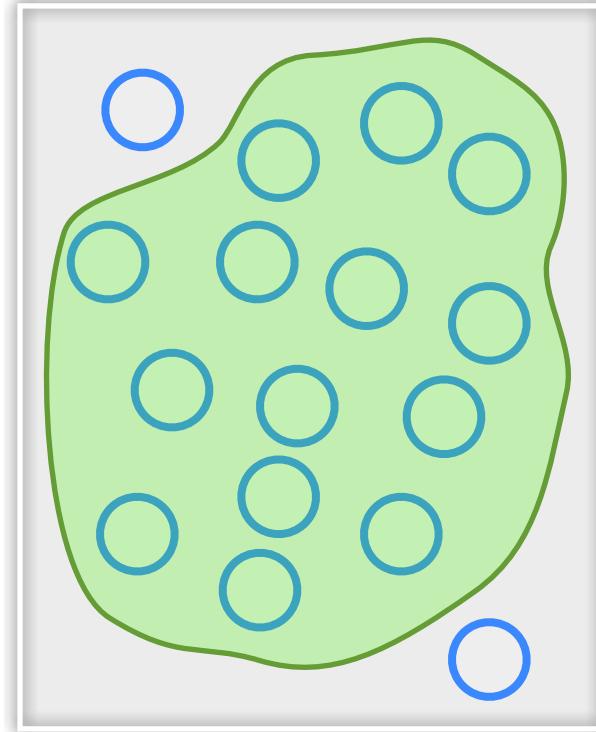
Select active

# Selective Mutation



# Selective Mutation

**Full Set:**  
Test cases that  
kill all mutants



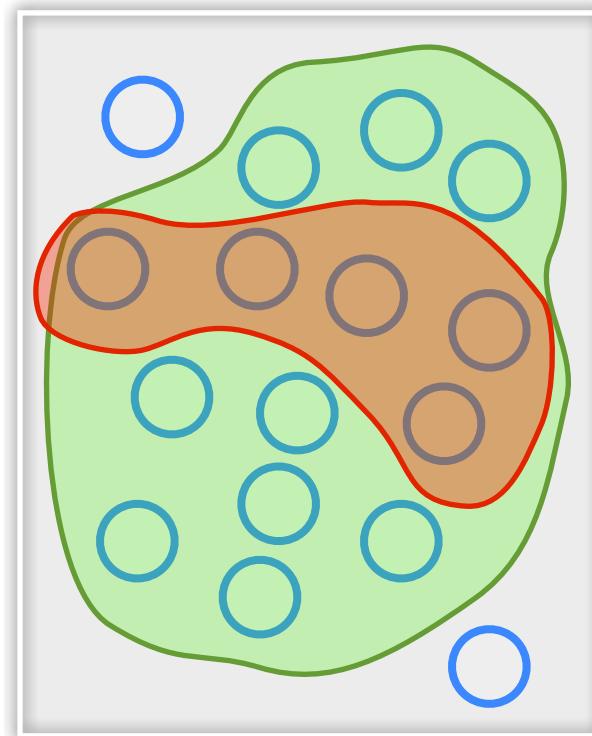
# Selective Mutation

## **Full Set:**

Test cases that  
kill all mutants

## **Sufficient Subset:**

Test cases that kill  
these mutants will  
kill all mutants



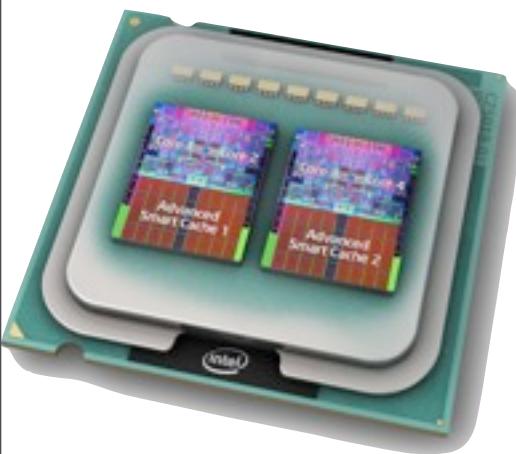
# Selective Mutation

- Use only a subset of mutation operators instead of all operators
- Subset is sufficient
- Detecting mutants of sufficient subset will detect >99% of all mutants
- ABS, AOR, COR, ROR, UOI

# Do Smarter/Faster

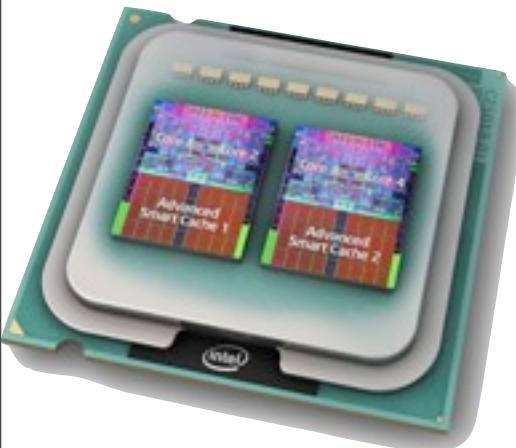
# Do Smarter/Faster

Mutation testing is  
inherently parallelizable



# Do Smarter/Faster

Mutation testing is inherently parallelizable



```
6: iload_1 // a
7: ifeq 14
10: iload_2 // b
11: ifne 23
14: iload_3 // c
15: ifeq 34
// ...
23: invokevirtual #4;
// ...
34: invokevirtual #5;
```

Mutating bytecode avoids recompilation

# Do Smarter/Faster

Mutation testing is inherently parallelizable



```
6: iload_1 // a  
7: ifeq 14  
10: iload_2 // b  
11: ifne 23  
14: iload_3 // c  
15: ifeq 34  
// ...  
23: invokevirtual #4;  
// ...  
34: invokevirtual #5;
```

Mutating bytecode avoids recompilation

Sample subset of mutants

