

Automated Testing & Verification

Richer type systems

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What are they good for?

- Classify/Filter programs
 - If a program does not type checks, then it is not part of the language
- Forbid undesirable behaviors
 - Adding “dates” to “words”
 - Unsafe handling of a pointer
- Force the usage of user-defined interfaces
 - Abstract types

Types

- What is a type?
 - Is a set of values of an expression
 - Example: $\text{int } x; \{x \in \mathbb{Z} \mid \text{MIN_INT} \leq x \leq \text{MAX_INT}\}$
 - Together with the operations that can be applied to these values
 - $\text{int } x$
 - $x + 4 : \text{int}$
 - $x + \text{“hello”}?$
- What is a type system?
 - A set of types and the rules for creating and using them.

Basic type checking

- The type checking follows the **syntactic structure** of the term to check
- There is an inference rule for each node in the syntax tree

$$\frac{\begin{array}{l} A \vdash E_1 : \text{int} \\ A \vdash E_2 : \text{int} \end{array}}{A \vdash E_1 + E_2 : \text{int (sum)}}$$

- Where $A \vdash E : T$ is a type judgement
 - given $A = [x_1 : T_1, \dots, x_n : T_n]$ a set of type assumptions, it can be derived from these typing rules that E is of type T
- We say a term is **well typed** if $[] \vdash E : T'$

Type-system rules example

- Terms:
 - a is a variable
 - $\dots, -1, 0, 1, \dots$ are integer expressions
 - $E + E$ is the addition
 - $T \text{ m}(T a) \{ \text{Body} \}$ is a method declaration
 - $m(E)$ is an invocation to method m

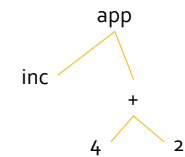
- T is a type

$\frac{A(a) = T}{A \vdash a : T \text{ (var)}}$	$\frac{A \vdash T2 \text{ m}(T1 a) \{ \dots \} : T1 \rightarrow T2 \quad A \vdash E : T1}{A \vdash m(E) : T2 \text{ (app)}}$
$\frac{n = \dots -1, 0, 1, \dots}{[] \vdash n : \text{int} \text{ (const)}}$	$\frac{A \vdash E1 : \text{int} \quad A \vdash E2 : \text{int}}{A \vdash E1 + E2 : \text{int} \text{ (sum)}}$

Type-system rules example

$\frac{A(a) = T}{A \vdash a : T \text{ (var)}}$	$\frac{A \vdash T2 \text{ m}(T1 a) \{ \dots \} : T1 \rightarrow T2 \quad A \vdash E : T1}{A \vdash m(E) : T2 \text{ (app)}}$	<pre>int m() { return inc(4+2); }</pre>
$\frac{n = \dots -1, 0, 1, \dots}{[] \vdash n : \text{int} \text{ (const)}}$	$\frac{A \vdash E1 : \text{int} \quad A \vdash E2 : \text{int}}{A \vdash E1 + E2 : \text{int} \text{ (sum)}}$	<pre>int inc(a: int) { return a+1; }</pre>

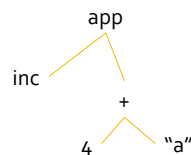
$\vdash 4 : \text{int} \text{ (const)} \quad \vdash 2 : \text{int} \text{ (const)}$
 $\vdash 4 + 2 : \text{int} \text{ (sum)} \quad \vdash \text{int inc}(a : \text{int}) \{ \dots \} : \text{int} \rightarrow \text{int}$
 $\vdash \text{inc}(4+2) : \text{int} \text{ (app)} \quad \checkmark$



Type-system rules example

$\frac{A(a) = T}{A \vdash a : T \text{ (var)}}$	$\frac{A \vdash T2 \text{ m}(T1 a) \{ \dots \} : T1 \rightarrow T2 \quad A \vdash E : T1}{A \vdash m(E) : T2 \text{ (app)}}$	<pre>int m() { return inc(4+"a"); }</pre>
$\frac{n = \dots -1, 0, 1, \dots}{[] \vdash n : \text{int} \text{ (const)}}$	$\frac{A \vdash E1 : \text{int} \quad A \vdash E2 : \text{int}}{A \vdash E1 + E2 : \text{int} \text{ (sum)}}$	<pre>int inc(a: int) { return a+1; }</pre>

$\vdash 4 : \text{int} \text{ (const)} \quad \vdash "a" : ?$
 $\vdash 4 + "a" : \text{Error! (sum)}$



Type Inference

- We call **erase(e)** to a function taking a "well-typed" e that returns e with no type-information.
- Given a non-typed term e_j : Is this the result of **erase(e)** for some e ? Which are the types of e ?
- This is the **type inference** problem. We have to find valid types instead of just checking their validity.

Type Inference

- Discover all type annotations such that the program typechecks.
 - Idea: Introduce unknowns to the rules and see if the rules can be solved consistently

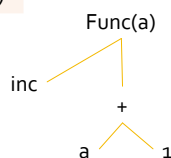
```
int m()
{
    return inc(4+2);
}

? inc(a: ?)
{
    return a+1;
}
```

$$\begin{array}{l} A \vdash E_1:\text{int} \\ A \vdash E_2:\text{int} \end{array}$$
$$A, x:T_1 \vdash E:T_2$$
$$A \vdash E_1 + E_2 : \text{int} \text{ (sum)}$$
$$A \vdash_{T_2} \text{func}(x:t_{T_1}) \{E\} : T_1 \rightarrow T_2 \text{ (func)}$$
$$\{a:\text{int}\} \vdash a:\text{int} \quad \vdash 1:\text{int}$$
$$\{a:A\} \vdash a+1:B = \text{int}(\text{sum})$$
$$\vdash \mathbf{B} \text{ inc}(a:\mathbf{A}) \{a+1; \}: \mathbf{A} \rightarrow \mathbf{B} \quad (\text{func})$$

```
A = int
B = int
```

```
|- int inc(a:int) {a+1;}
```



A richer type system

- Idea: Use types to filter out programs with undesirable behavior
- Examples:
 - Potential runtime exceptions
 - Non-null types
 - Security/Protection
 - Reference immutability / ownership types
 - A certain protocol is not obeyed
 - Type states

Non-null types

```
class C {
    D f;

    C() {
        if (b)
            f =
        }
    }

    C(D x)
        f = x
    }

    void m(
        f.
    )
}
```

Was f really initialized?

- It depends on a condition

Does f point to an object?

- It depends on the value x

Can field f be null?

Non-null types

```
class C {
    D! f;
    C() {
        if (bluemoon()) {
            f = new D();
        }
    }
    C(D x) {
        f = x;
    }
    void m() {
        f.q();
    }
}
```

- Field f is non-null !

Now the errors are explicit

- 1. Paths do not initialize f
- 2. x can **not** be assigned to f

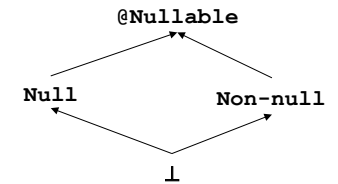
Now if a program typecheck,
then it guarantees no null
dereference.

Non-null Annotation

- Extend the type system to:
 - Improve documentation
 - Record intention
- Usage:
 - Detect errors during source compilation
 - Detect errors sooner, possibly before dereference
 - Low the number of runtime exceptions
 - Optimization
 - Useful for other analysis

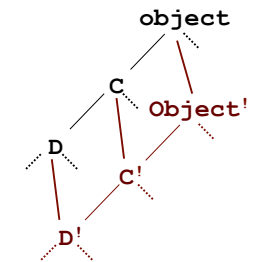
Extensions

- Types given a class T
 - Non-null: $T!$ ($@nonNull T$)
 - Possibly-null: T ($@Nullable T$)



- Use $T!$ for arguments, return, fields, variables ...

- Explicit type cast from T to $T!$
- New type hierarchy
- Changes in semantic of constructors



Examples

```
T! t = new T(...); // create an object of type non-null
T n = t;           // OK: nullable super type of non-null
...
if (n != null)
    t = n;          // here n has type T!
t = (T!)n;         // requires a cast (runtime check)
int x = t.f;        // requires t non-null
...
t.m(...);           // requires t non-null
...
throw t;            // requires t non-null
```

Problems

- Component initialization (constructors, arrays)
 - Default reference initialization is to null!
- Constructors must enforce object invariants
 - Each non-null field must be initialized
- Do we grant access to partially initialized objects?
 - No: simpler, but more limited
 - No method invocation is allowed from the constructor!
 - Yes: what is the type for those objects?

Example

```
class A {
  string! name;
  public A(string! s) {
    this.name = s;
    this.m(55);
  }
  virtual void m(int x) { ... }
}
```

OK: **name** is
initialized before its
use

Example (cont.)

```
class B : A {
  string! path;
  public B(string! p, string! s)
    : base(s) {
    this.path = p;
  }

  override void m(int x) {
    ... a = this.path ...
  }
}
```

m() is invoked from A's
constructor, before B()
initialized **path**!

```
class A {
  string! name;
  public A(string! s) {
    this.name = s;
    this.m(55);
  }
  virtual void m(int x) { ... }
}
```

Solution

- The “raw” type
 - $x : T^{\text{raw!}}$ object partially initialized of type T
 - A constructor can only call methods accepting Raw data types.
- For raw objects, the rules reading and writing fields change:
 - Given $x : T^{\text{raw!}}$. If the field $x.f$ has type $C!$:
 - `read(t = x.f)` returns $t : C$ (it might be null)
 - `write(x.f = b)` **requires** $b : C!$ (whatever we write, it might be non-null)



Example

```
class A {
  string! name;
  public A(string! s) {
    this.name = s;
    this.m(55);
  }

  [Raw]
  virtual void m(int x) { ... }
}
```

```
class B : A {
  string! path;
  public B(string! p, string! s)
    : base(s) { this.path = p; }

  [Raw]
  override void m(int x) {
    ... a = this.path ...
  }
}
```

Now a is @Nullable
So any dereference of a fails!

An implementation

- Spec# type system
 - <http://research.microsoft.com/en-us/projects/specsharp/>

A richer type system

- Idea: Use types to filter out programs with undesirable behavior
- Examples:
 - Potential runtime exceptions
 - Non-null types
 - Security/Protection
 - Reference immutability / ownership types
 - A certain protocol is not obeyed
 - Type states

Reference immutability

- Any problem with this program?

```
class C {  
    private int data;  
  
    public int getData() {  
        return data;  
    }  
}  
  
int i = myClass.getData();  
i++;
```

Reference immutability

- And with this program?

```
class C {  
    private string data;  
  
    public string getData() {  
        return data;  
    }  
}  
  
String s = myClass.getData();  
s.trim();
```

Reference immutability

- And with this one?

```
class C {  
    private List data;  
  
    public List getData() {  
        return data;  
    }  
}  
  
List l = myClass.getData();  
l.add();
```

- **Mutation error:** a side-effect leads to an undesired update.

Information Leak

- A security leak in JDK 1.1

```
class Class {  
    private Object[] signers;  
    Object[] getSigners() {  
        return signers;  
    }  
}
```

Example

- A possible solution

```
class C {  
    private List data;  
  
    public List getData() {  
        return new List(data);  
    }  
}  
  
List l = myClass.getData();  
l.add();
```

- Is this what we want?
- Is always that simple?

- It does not seem to be a feasible solution

Enriching our type system

- We might indicate that a given reference is immutable

```
class C {  
    private List data;  
  
    public @ReadOnly List getData() {  
        return data;  
    }  
}  
  
List l = myClass.getData();  
l.add(); // compilation error!
```

Protecting arguments

```
public void m(Graph g) {  
    ...  
    g.addEdge(n1,n2);  
}
```

- We want to **forbid** changes to *g*

```
public void m(final Graph g) {  
    ...  
    g.addEdge(n1,n2);  
}
```

- Is this enough?
- No! "final" only avoids a reference from being **modified**.

```
public void m(@ReadOnly Graph g) {  
    ...  
    g.addEdge(n1,n2); // compilation error  
}
```

- Is it enough now?
- Yes! ReadOnly protects the reference

Kinds of Immutability

- **Object immutability**: an object can not be modified by **any** reference

```
Graph temp = new Graph();
```

```
// construct the graph
```

```
readonly Graph g = temp;  
temp = null;
```

- **Reference immutability**: independent control for each reference

Abstract state mutation

- **Mutation**: any change to the abstract state of the object.
 - Abstract state: by default all fields. Some fields can be excluded. The abstract state is recursive over all reachable objects.
- Two control mechanisms:
 - Mutability
 - Assignability

Mutability

- It defines if the (abstract) state of an object can be modified.

```
class Date {  
    int year;  
}
```

```
/*mutable*/ Date d;  
readonly Date rd;  
d.year = 2005; // OK  
rd.year = 2005; // Error
```

Mutability annotations

- They are applied on fields and variables
- **readonly**: The referent abstract state can not be modified
- **mutable**: The abstract state can be modified
 - Default for all local variables
- **this-mutable**: (all for fields)
 - Mutability depends on container class
 - It can be modified if the container instance is mutable
 - It can't be modified if the container class is read-only
 - *this.f* is mutable if *this* is mutable and *f* is this-mutable
 - *this.f* is readonly if *this* is readonly y *f* is this-mutable

Mutability vs. Assignability

- **Mutable**
 - It is a part of the type
 - **readonly**
- **Assignable**
 - It's not a part of the type
 - **final**

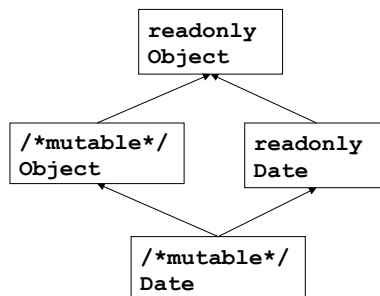
```
final      Date fd = null;
@readonly Date rd = null;
```

```
fd = new Date(); // Error: final
rd = null;       // OK
```

```
Date d1 = fd; // OK
Date d2 = rd; // Error: wrong type
```

Type system

- Each (mutable) type **T** has **readonly T** as super type
 - In other words, we can assign a mutable to a readonly reference, but not the other way around.



readonly

```
class Account {
    @ReadOnly Customer owner;
    @Mutable RequestLog requests;
    Balance bal; //def:this-mutable
}
...
Account a; //def:mutable
@ReadOnly Account ra;
a.owner.setName("Bob"); // Error
ra.owner.setName("Bob"); // Error
```

Mutability of ref.f		
Declared mutability of f	Resolved mutability of ref	
	mutable	readonly
readonly	readonly	readonly

mutable

```
class Account {
    @ReadOnly Customer owner;
    @Mutable RequestLog requests;
    Balance bal; //def:this-mutable
}
...
Account a; //def:mutable
@ReadOnly Account ra;
a.requests.add("checkBalance"); // OK
ra.requests.add("checkBalance"); // OK
```

mutable excludes **requests** from the abstract state of the object.

Mutability of ref.f		
Declared mutability of f	Resolved mutability of ref	
	mutable	readonly
readonly	readonly	readonly
mutable	mutable	mutable

this-mutable

```
class Account {
    @ReadOnly Customer owner;
    @Mutable RequestLog requests;
    Balance bal; //def:this-mutable
}
...
Account a; //def:mutable
@ReadOnly Account ra;
a.balance.withdraw(1000); // OK
```

this-mutable: the mutability of **bal** depends on the mutability of this

Mutability of ref.f		
Declared mutability of f	Resolved mutability of ref	
	mutable	readonly
readonly	readonly	readonly
mutable	mutable	mutable
this-mutable	mutable	<? readonly>

this-mutable

```
class Account {
    @ReadOnly Customer owner;
    @Mutable RequestLog requests;
    Balance bal; //def:this-mutable
}
...
Account a; //def:mutable
@ReadOnly Account ra;
a.balance.withdraw(1000); // OK
ra.balance.withdraw(1000); // Error
```

this-mutable: the mutability of **bal** depends on the mutability of this

Mutability of ref.f		
Declared mutability of f	Resolved mutability of ref	
	mutable	readonly
readonly	readonly	readonly
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this-mutable	mutable	<? readonly>

Recap

```
class Account {
    @ReadOnly Customer owner;
    @Mutable RequestLog requests;
    Balance bal; //def:this-mutable
}
...
Account a; //def:mutable
@ReadOnly Account ra;
```

Mutability of ref.f		
Declared mutability of f	Resolved mutability of ref	
	mutable	readonly
readonly	readonly	readonly
mutable	mutable	mutable
this-mutable	mutable	<? readonly>

```
a.owner.setName("Bob"); // Error
ra.owner.setName("Bob"); // Error
a.requests.add("checkBalance"); // OK
ra.requests.add("checkBalance"); // OK
a.balance.withdraw(1000); // OK
ra.balance.withdraw(1000); // Error
```

Assignability

Assignability (ref . f)		
Declared assignability of f	Mutability (ref)	
	mutable	readonly
final	no-assignable	no-assignable
assignable	assignable	assignable
this-assignable	assignable	no-assignable

```
class Bicycle {
    final int id;
    @Assignable int hashCode;
    int gear; //def:this-assignable
}
Bicycle b; //def:mutable
@ReadOnly Bicycle rb;
```

- b.id = 5;
- rb.id = 5;
- b.hashCode = 5;
- rb.hashCode = 5;
- b.gear = 5;
- rb.gear = 5;

Assignability

Assignability (ref . f)		
Declared assignability of f	Mutability (ref)	
	mutable	readonly
final	no-assignable	no-assignable
assignable	assignable	assignable
this-assignable	assignable	no-assignable

```
class Bicycle {
    final int id;
    @Assignable int hashCode;
    int gear; //def:this-assignable
}
Bicycle b; //def:mutable
@ReadOnly Bicycle rb;
```

- b.id = 5;
- rb.id = 5;
- b.hashCode = 5;
- rb.hashCode = 5;
- b.gear = 5;
- rb.gear = 5;

Problematic example

```
class Student {
    @Assignable GradeReport grades; //this-mutable
}

myMethod(@ReadOnly GradeReport rg ...) {
    Student s = new Student(); //mutable
    @ReadOnly Student rs = s;

    GradeReport g; //mutable

    rs.grades = rg;
    g = s.grades;
}
```

- A this-mutable reference from readonly should be readonly?

Problematic example

```
class Student {
    @Assignable GradeReport grades; //this-mutable
}

myMethod(@ReadOnly GradeReport rg...) {
    Student s = new Student(); //mutable
    @ReadOnly Student rs = s; // Valid

    GradeReport g; //mutable

    rs.grades = rg; //readonly assigned to this-mutable
    g = s.grades; // now g has rg as mutable!
}
```

- A this-mutable reference from readonly should be readonly?
 - No! It might turn a readonly reference to a mutable reference without explicitly stating that.

This-mutables refs from readonly refs

- Solution: Forbid a readonly reference from being copied to a this-mutable field.

```
class Student {  
    assignable /*this-mut*/ GradeReport grades;  
}
```

This-mutable fields are:

- **Read** as **readonly** GradeReport
- **Written** as **mutable** GradeReport

```
rs.grades = rg; // error! readonly (rg) assigned to a  
    mutable (rs.grades)
```

Javari

- Javari is a backward-compatible extension of the Java language.
- The programmer can specify that a particular reference is read-only
 - Cannot be used to change the state of its referent
- Javari compile-time checker verifies this property.

Javari: reference immutability

- A **reference** is immutable if we can not use this reference to modify the object
 - Others references might modify it
- An extension of the type system to deal with updates through references.
- “Depth” immutability control
 - All the reachable state

Javari

- **Static typing**
 - It is checked at compilation time
 - Type casting delegates checking at execution time
- **Uses**
 - Documentation checkable by a computer
 - Prevent/detect errors
 - Useful information for other analyses

A richer type system

- Idea: Use types to filter out programs with undesirable behavior
- Examples:
 - Potential runtime exceptions
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 - Security/Protection
 - Reference immutability / ownership types
- A certain protocol is not obeyed
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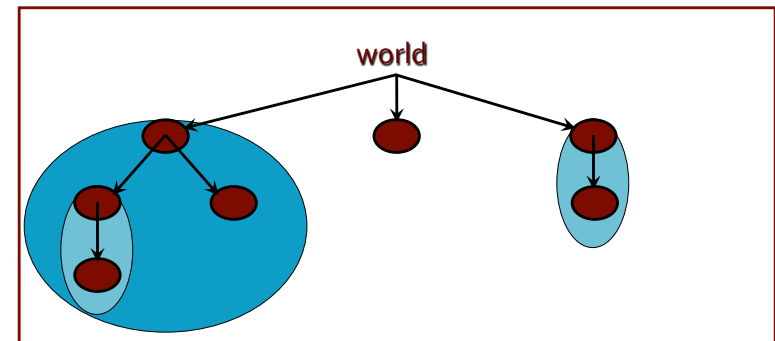
Encapsulation

- **Encapsulation:** Restrict access to object internal representation
 - The inner state of an object is hidden to the external objects
- Goals:
 - Independent from representation
 - Side-effects (preserve invariants)
 - Modular reasoning
 - Think of objects as components
 - Fundamental for reasoning on complex systems
 - And also for automatic analysis!
 - Security

Ownership types

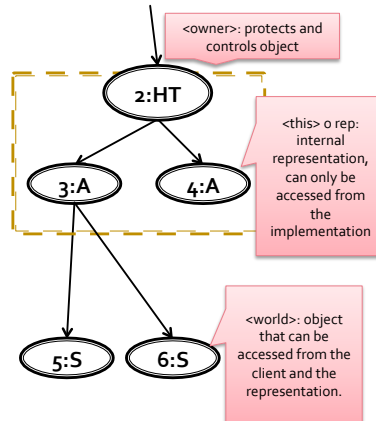
- Types for Flexible Alias protection
- **Property:** Each object has an owner
 - Owners control access to objects
- Use **type-checking** to enforce this property on the programs

Ownership Types



Types for alias protection

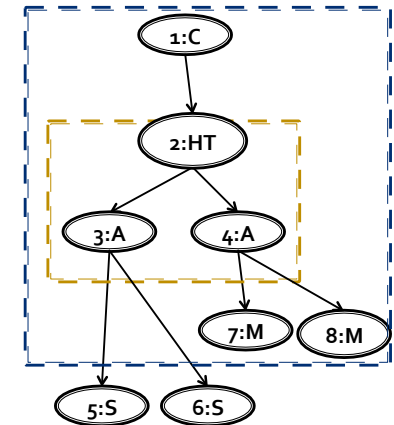
```
class HT<o, k, i> {
  private Array<this,k> keys;
  private Array<this,i> items;
  public void put(H<k> key, O<i> value);
  public O<i> get(H<k> key);
}
class Student {
}
```



- The first parameter is the owner
- <this> means internal representation object (also rep)
- <o> Owner passed as parameter
- <world> Default, means no restrictions

Types for alias protection

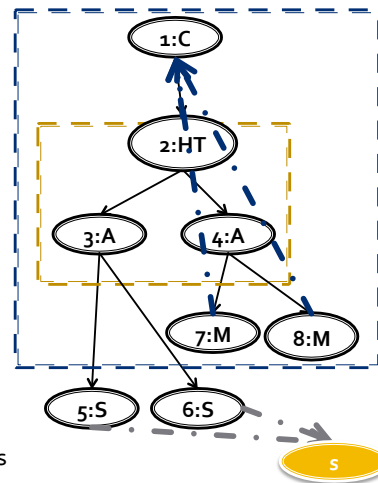
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  private Array<this,k> keys;
  private Array<this,i> items;
  public void put(H<k> key, O<i> value);
  public O<i> get(H<k> key);
}
class Student {
}
class Mark {
}
class Course<s> {
  HT<this,s,this> marks;
}
```



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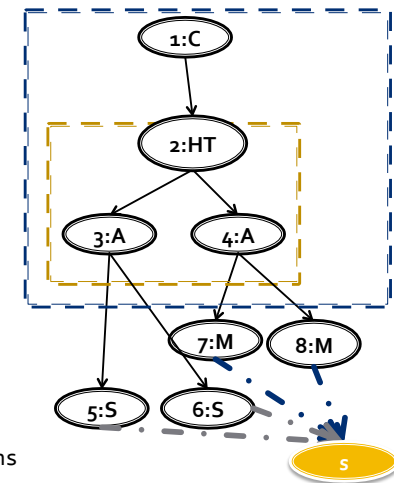
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- <world> Default, means no restrictions

A richer type system

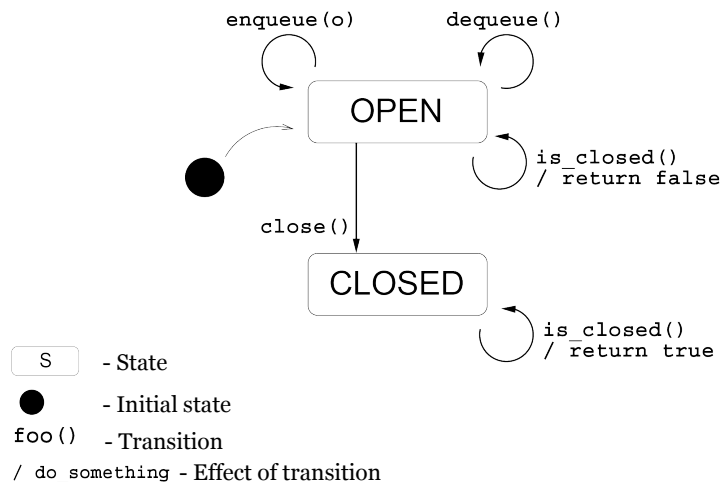
- Idea: Use types to filter out programs with undesirable behavior
- Examples:
 - Potential runtime exceptions
 - Non-null types
 - Security/Protection
 - Reference immutability / ownership types
 - A certain protocol is not obeyed
 - Type states

API protocols

- Increasing complexity of APIs
 - Dozens or hundreds of functions
 - Not always well documented
- Programs are more dependent on them
 - Framework APIs
 - Library APIs
 - Database connections APIs, etc.
- **Problem:** how to correctly use them?



Example: queue

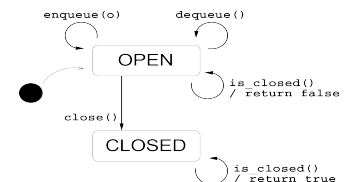


Typestate: dynamic types

- A typestate is a dynamic version of a type

Traditional Type	Typestate
Indicates what actions are allowed on an instance.	Indicates what actions are allowed on an instance at a given instant

- Each state in a typestate prunes functionality



Controlling access to an object

```
public static void f1(@Unique Object myObj) {
    // myObj is the only reference to the object
}

public static void f2(@Full Object myObj) {
    // we can modify the state of myObj
    // (only "read-only" references can exist)
}

public static void f3(@Pure Object myObj) {
    // we can not modify the state of myObj
    // (other references may modify it)
}

public static void f4(@Share Object myObj) {
    // we can modify myObj
    // (other share references can also modify it)
}
```

Permissions can be modified
 @Unique => 1x@Full & Nx@Pure
 @Full => Nx@Imm
 @Full => Nx@Share & Mx@Pure
 ...

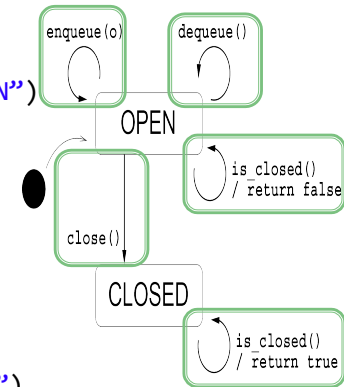
A queue protocol

```
@Full(requires="OPEN", ensures="CLOSED")
void close()
```

```
@Full(requires="OPEN", ensures="OPEN")
void enqueue(@Share Object o)
```

```
@Pure
@TrueIndicates("CLOSED")
@FalseIndicates("OPEN")
boolean is_closed()
```

```
@Pure(requires="OPEN", ensures="OPEN")
Object dequeue()
```

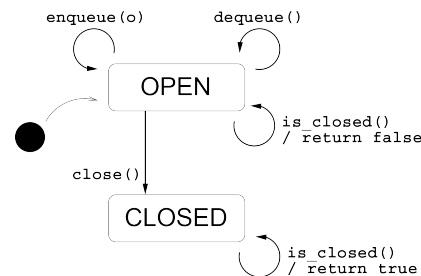


Analyzing Queue usage

```
final Blocking_queue queue = new Blocking_queue();
// OPEN

for( int i=0;i<5;i++ )
    // OPEN
    queue.enqueue("Object " + i);
    // OPEN

queue.close();
// CLOSED
```



Queue and multithreads...

```
final Blocking_queue queue = new Blocking_queue();

(new Thread() {
    @Override
    public void run() {
        while( !queue.is_closed() )
            System.out.println("Got object: "+queue.dequeue());
        System.exit();
    }}).start();

for( int i=0;i<5;i++ )
    queue.enqueue("Object" + i);

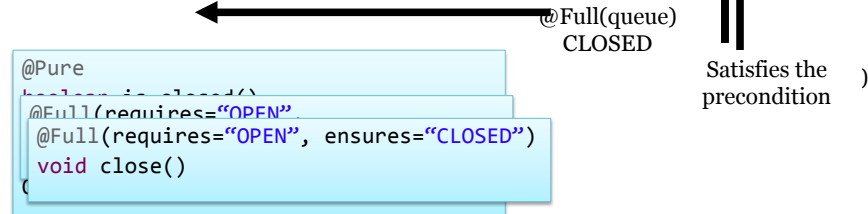
queue.close();
```

Any problem?

Race condition

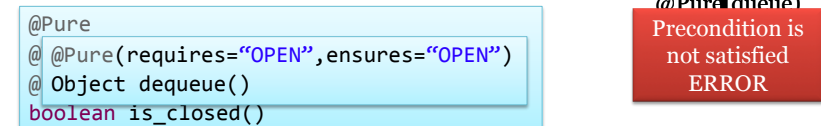
Verifying Producer

```
final Blocking_queue queue = new Blocking_queue();
// @Unique(queue) OPEN
(...).start();
// @Full(queue) OPEN
for( int i=0;i<5;i++ )
    queue.enqueue("Object " + i);
// @Full(queue) OPEN
queue.close();
```



Verifying Consumer

```
@Override
public void run() {
    // @Pure(queue)
    while( !queue.is_closed() )
        // @Pure(queue)
        System.out.println("Got object: " +
            queue.dequeue());
    System.exit();
}
```



Plural (Aldrich et al.)

- Eclipse plugin
 - <http://code.google.com/p/pluralism/>
- Typechecking is done through dataflow
 - Modular: type annotations
- User is able to specify:
 - Access permissions (*aliasing control*)
 - Object abstract states (*typestates*)