

A Comparison of Constraint-based and Sequence-based Generation of Complex Input Data Structures

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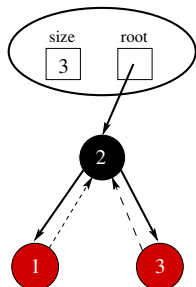
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Example Complex Data Structures

- Data structures that have linked nodes whose values need to satisfy some complex constraints

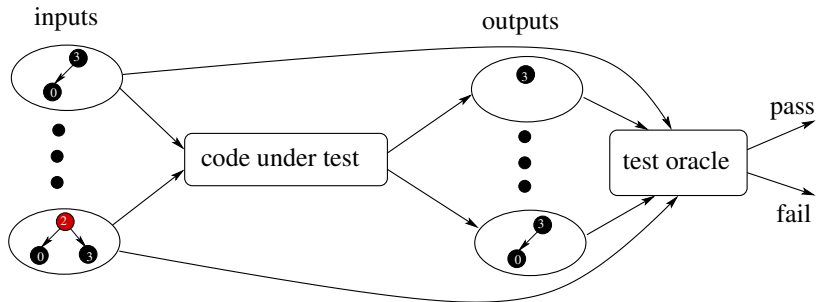
RedBlackTree



AST of Java Program

```
class A implements B {  
    public A m() {  
        A a = null;  
        return a;  
    }  
}  
  
interface B extends C {  
    public B m();  
}  
  
interface C {  
    public C m();  
}
```

Testing Setup



- Example scenarios:
 - Testing “remove” on “RedBlackTree” (input: RBTs)
 - Testing compiler or refactoring engine (input: programs)
- Our focus: Generation of test inputs

Bounded-Exhaustive Testing

Automated testing approach that checks a system under test for **all inputs** within given bounds

- Rationale: small-scope hypothesis [Jackson & Damon ISSTA 96]
- Exhaustive testing within bounds catches “corner cases”

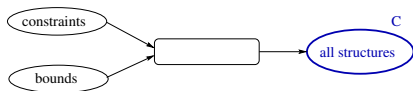
Used in academia and industry to test real-world applications

- Refactoring Engines - Eclipse & NetBeans [Daniel et al. FSE 07]
- Web Traversal Agent from Google [Misailovic et al. FSE 07]
- XPath Compiler at Microsoft [Stobie ENTCS 05]
- Constraint Analyzer [Khurshid & Marinov J-ASE 04]
- Fault-Tree Analyzer for NASA [Sullivan et al. ISSTA 04]
- Protocol for Dynamic Networks [Khurshid & Marinov ENTCS 01]

Two Approaches for Automated Generation

■ Constraint-based Generation

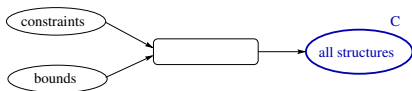
- Describe data structure constraints and provide bounds
- Solve constraints
- Generate structures at the concrete representation level



Two Approaches for Automated Generation

■ Constraint-based Generation

- Describe data structure constraints and provide bounds
- Solve constraints
- Generate structures at the concrete representation level



■ Sequence-based Generation

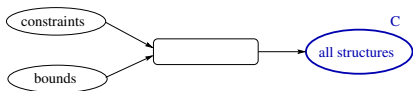
- Use sequences of methods
- Provide length of sequence and parameter values
- Generate structures at the abstract level



Two Approaches for Automated Generation

■ Constraint-based Generation

- Describe data structure constraints and provide bounds
- Solve constraints
- Generate structures at the concrete representation level



■ Sequence-based Generation

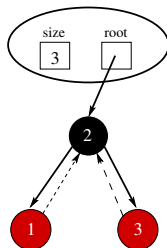
- Use sequences of methods
- Provide length of sequence and parameter values
- Generate structures at the abstract level



- Compare structures in C and S

Example - RedBlackTree

```
class RedBlackTree {  
    int size;  
    Node root;  
  
    static boolean RED = false;  
    static boolean BLACK = true;  
  
    static class Node {  
        Node left, right, parent;  
        boolean color;  
        int value;  
    }  
  
    RedBlackTree() { /* empty tree */ }  
  
    void insert(int value) { ... }  
    void remove(int value) { ... }  
}
```



Example - Generated Structure

```
// constraint based
```

```
RedBlackTree rbt = new RedBlackTree();
```

```
Node n0 = new Node();
```

```
Node n1 = new Node();
```

```
Node n2 = new Node();
```

```
n0.color = BLACK;
```

```
n0.value = 2;
```

```
n0.left = n1;
```

```
n0.right = n2;
```

```
n0.parent = null;
```

```
n1.color = RED;
```

```
n1.value = 1;
```

```
n1.left = null;
```

```
n1.right = null;
```

```
n1.parent = n0;
```

```
n2.color = RED;
```

```
n2.value = 3;
```

```
n2.left = null;
```

```
n2.right = null;
```

```
n2.parent = n0;
```

```
// sequence based
```

```
RedBlackTree rbt = new RedBlackTree();
```

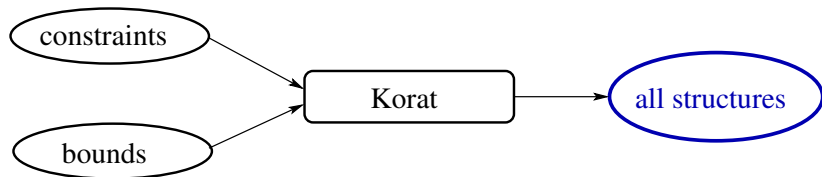
```
rbt.insert(2);
```

```
rbt.insert(1);
```

```
rbt.insert(3);
```

Constraint-based Generation: Korat

- <http://mir.cs.illinois.edu/korat>
- Input:
 - Constraints (written in standard implementation language)
 - Bound
- Output:
 - All structures where constraints are satisfied



Constraint-based Generation: Bounds

- User provides bounds

RBT

size	root
<input type="text"/>	<input type="text"/>

Constraint-based Generation: Bounds

- User provides bounds

RBT

size	root
<input type="text"/>	<input type="text"/>

3

N0

left	right	parent	color	value
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>

N1

left	right	parent	color	value
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>

N2

left	right	parent	color	value
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>

Constraint-based Generation: Bounds

- User provides bounds

RBT

size	root
<input type="text"/>	<input type="text"/>

3 null
 N0
 N1
 N2

N0				
left	right	parent	color	value
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
null	null	null		
N0	N0	N0		
N1	N1	N1		
N2	N2	N2		

N1				
left	right	parent	color	value
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
null	null	null		
N0	N0	N0		
N1	N1	N1		
N2	N2	N2		

N2				
left	right	parent	color	value
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
null	null	null		
N0	N0	N0		
N1	N1	N1		
N2	N2	N2		

Constraint-based Generation: Bounds

- User provides bounds

RBT

size	root
<input type="text"/>	<input type="text"/>

3 null
 N0
 N1
 N2

N0				
left	right	parent	color	value
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
null	null	null	true	1
N0	N0	N0	false	2
N1	N1	N1		3
N2	N2	N2		

N1				
left	right	parent	color	value
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
null	null	null	true	1
N0	N0	N0	false	2
N1	N1	N1		3
N2	N2	N2		

N2				
left	right	parent	color	value
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
null	null	null	true	1
N0	N0	N0	false	2
N1	N1	N1		3
N2	N2	N2		

Constraint-based Generation: Bounds

- Korat automatically generates the structures

RBT

size	root
3	N0

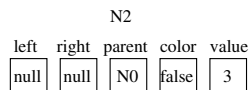
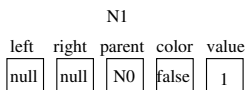
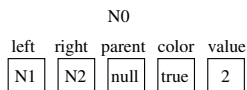
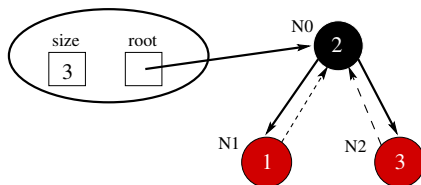
N0				
left	right	parent	color	value
N1	N2	null	true	2

N1				
left	right	parent	color	value
null	null	N0	false	1

N2				
left	right	parent	color	value
null	null	N0	false	3

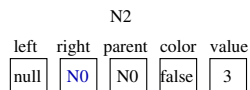
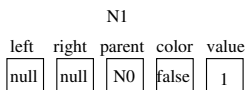
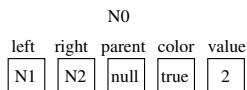
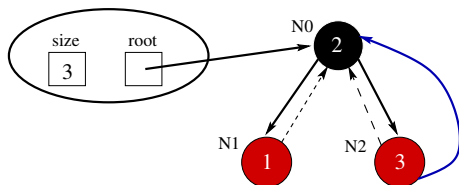
Constraint-based Generation: Bounds

- Korat automatically generates the structures



Constraint-based Generation: Bounds

- Korat automatically generates the structures



- Korat checks the constraints on each candidate structure

```
boolean repOk() {  
    return treeness() && coloring() && ordering();  
}
```

- Treeness
 - No cycles
 - No two incoming edges to the same node
 - All nodes must be reachable from the root
- Coloring
 - Red node cannot have red children
 - Paths have the same number of black nodes
- Ordering
 - Nodes value ordered for binary search

Constraint-based Generation: Constraints

```
boolean treeness() {
    if (root == null) return size == 0;
    Set<Node> visited = new HashSet<Node>();
    visited.add(t.root);
    List<Node> workList = new LinkedList<Node>();
    workList.add(t.root);
    if (root.parent != null) return false;
    while (!workList.isEmpty()) {
        Node current = workList.removeFirst();
        Node cl = current.left;
        if (cl != null) {
            if (!visited.add(cl)) return false;
            if (cl.parent != current) return false;
            workList.add(cl);
        }
        Node cr = current.right;
        if (cr != null) {
            if (!visited.add(cr)) return false;
            if (cr.parent != current) return false;
            workList.add(cr);
        }
    }
    return size == visited.size();
}
```

Constraint-based Generation: Constraints

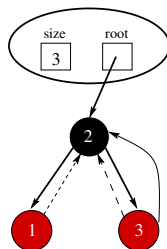
```
boolean treeness() {
    if (root == null) return size == 0;
    Set<Node> visited = new HashSet<Node>();
    visited.add(t.root);
    List<Node> workList = new LinkedList<Node>();
    workList.add(t.root);
    if (root.parent != null) return false;
    while (!workList.isEmpty()) {
        Node current = workList.removeFirst();
        Node cl = current.left;
        if (cl != null) {
            if (!visited.add(cl)) return false; // no cycles & no two incoming edges
            if (cl.parent != current) return false;
            workList.add(cl);
        }
        Node cr = current.right;
        if (cr != null) {
            if (!visited.add(cr)) return false; // no cycles & no two incoming edges
            if (cr.parent != current) return false;
            workList.add(cr);
        }
    }
    return size == visited.size();
}
```

Constraint-based Generation: Constraints

```
boolean treeness() {
    if (root == null) return size == 0;
    Set<Node> visited = new HashSet<Node>();
    visited.add(t.root);
    List<Node> workList = new LinkedList<Node>();
    workList.add(t.root);
    if (root.parent != null) return false;
    while (!workList.isEmpty()) {
        Node current = workList.removeFirst();
        Node cl = current.left;
        if (cl != null) {
            if (!visited.add(cl)) return false;
            if (cl.parent != current) return false;
            workList.add(cl);
        }
        Node cr = current.right;
        if (cr != null) {
            if (!visited.add(cr)) return false;
            if (cr.parent != current) return false;
            workList.add(cr);
        }
    }
    return size == visited.size(); // all nodes reachable
}
```

Constraint-based Generation: Constraints

```
boolean treeness() {  
    if (root == null) return size == 0;  
    Set<Node> visited = new HashSet<Node>();  
    visited.add(t.root);  
    List<Node> workList = new LinkedList<Node>();  
    workList.add(t.root);  
    if (root.parent != null) return false;  
    while (!workList.isEmpty()) {  
        Node current = workList.removeFirst();  
        Node cl = current.left;  
        if (cl != null) {  
            if (!visited.add(cl)) return false;  
            if (cl.parent != current) return false;  
            workList.add(cl);  
        }  
        Node cr = current.right;  
        if (cr != null) {  
            if (!visited.add(cr)) return false;  
            if (cr.parent != current) return false;  
            workList.add(cr);  
        }  
    }  
    return size == visited.size();  
}
```



- Pros:
 - Does not require all methods on data structure
 - Can test one method in isolation
- Cons:
 - Relies on the user to provide constraints
 - Can generate false alarms or miss bugs

- Structures are generated from sequences of methods
- Structures are created at the abstract level
- Concrete representation is considered to prune generation

```
RedBlackTree rbt = new RedBlackTree();
```

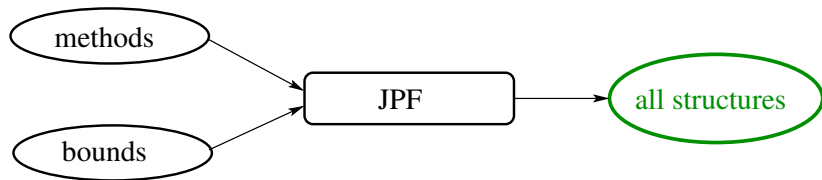
```
rbt.insert(1);  
rbt.remove(1);
```

```
RedBlackTree rbt = new RedBlackTree();
```

```
rbt.insert(2);  
rbt.remove(2);
```


JavaPath Finder (JPF)

- Stateful model checker for Java programs
- JPF is JVM with backtracking capabilities
- `Verify.getInt(int min, int max)`



Sequence-based Generation

```
class RedBlackTreeDriver {  
    static void main(String[] args) {
```

```
        RedBlackTree rbt = new RedBlackTree();
```

```
        switch (Verify.getInt(0, 1)) {  
            case 0:  
                rbt.insert(/* select value */);  
                break;  
            case 1:  
                rbt.remove(/* select value */);  
                break;  
        }
```

```
    }  
}
```

Sequence-based Generation

```
class RedBlackTreeDriver {
    static void main(String[] args) {

        // length of sequence (and method parameters)
        int lenOfSeq = ...;

        RedBlackTree rbt = new RedBlackTree();
        for (int i = 0; i < lenOfSeq; i++) {
            switch (Verify.getInt(0, 1)) {
                case 0:
                    rbt.insert(/* select value */);
                    break;
                case 1:
                    rbt.remove(/* select value */);
                    break;
            }
        }
    }
}
```

Sequence-based Generation

```
class RedBlackTreeDriver {
    static void main(String[] args) {

        // length of sequence (and method parameters)
        int lenOfSeq = ...;

        RedBlackTree rbt = new RedBlackTree();
        for (int i = 0; i < lenOfSeq; i++) {
            switch (Verify.getInt(0, 1)) {
                case 0:
                    rbt.insert(Verify.getInt(0, lenOfSeq - 1));
                    break;
                case 1:
                    rbt.remove(Verify.getInt(0, lenOfSeq - 1));
                    break;
            }
        }
    }
}
```

Sequence-based Generation

```
class RedBlackTreeDriver {
    static void main(String[] args) {
        int numOfNodes = ...;
        // length of sequence (and method parameters)
        int lenOfSeq = ...;

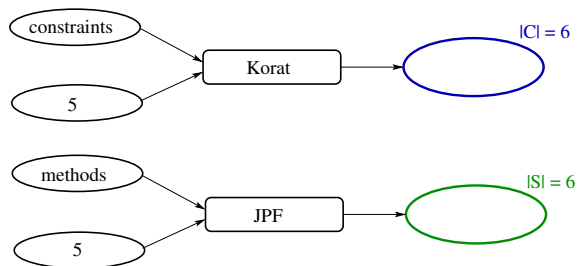
        RedBlackTree rbt = new RedBlackTree();
        for (int i = 0; i < lenOfSeq; i++) {
            switch (Verify.getInt(0, 1)) {
                case 0:
                    rbt.insert(Verify.getInt(0, lenOfSeq - 1));
                    break;
                case 1:
                    rbt.remove(Verify.getInt(0, lenOfSeq - 1));
                    break;
            }
        }
        if (rbt.size == numOfNodes) {
            printStructure(rbt);
        }
    }
}
```

- Pros:
 - Generates only the states reachable by sequences of methods
 - Cannot generate false alarms
- Cons:
 - Requires testing several methods at once
 - Test the method that we use to generate the structure

- Compare structures in C and S
- Five data structures with complex constraints
 - AVL Tree (put, remove)
 - HeapArray (insert, remove)
 - FibonacciHeap (insert, remove)
 - RedBlackTree (insert, remove)
 - DisjSet (find, union)
- Constraints (repOk) written “naturally”

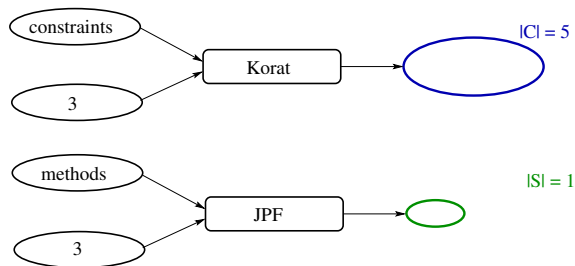
Case 1: Same Structures

- Same structures of size n with sequences of length n
- AVL Tree & HeapArray
- $C = S$



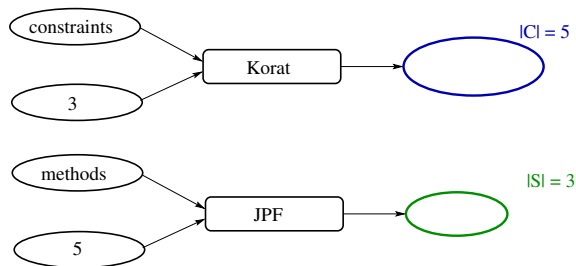
Case 2: Longer Sequences

- Same structures but longer sequences are required
- FibonacciHeap
- $C \supset S$



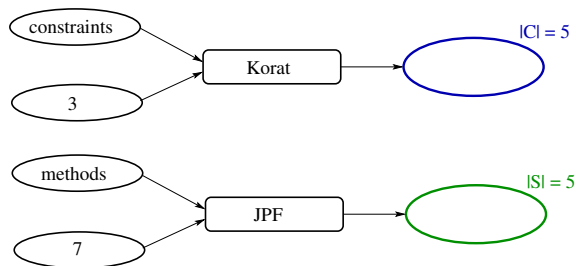
Case 2: Longer Sequences

- Same structures but longer sequences are required
- FibonacciHeap
- $C \supset S$



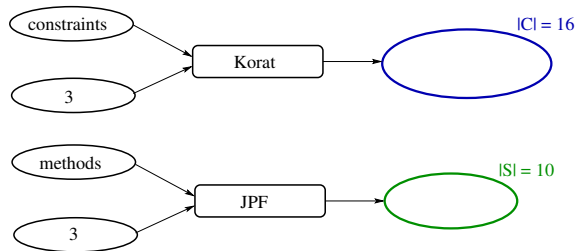
Case 2: Longer Sequences

- Same structures but longer sequences are required
- FibonacciHeap
- $C = S$



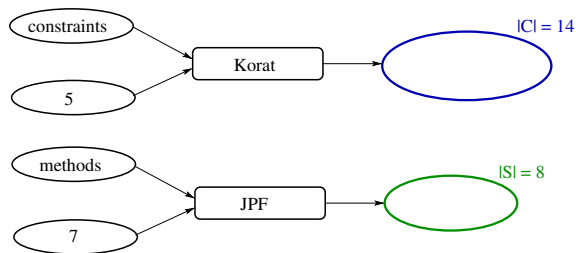
Case 3: More Structures, No False Alarms

- Constraint-based generates more structures but code under test works
- DisjSet
- $C \supset S$



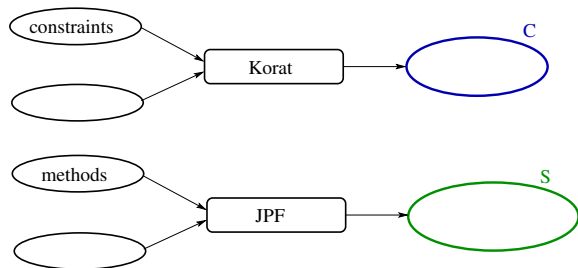
Case 4: More Structures, False Alarms

- Constraint-based generates more structures that lead to false alarm(s)
- RedBlackTree
- Slightly different implementation of the same data structure can behave differently in testing
- $C \supset S$



Case 5: Fewer Structures

- Constraint-based generates fewer structures, which could lead to missed bugs
- The case not encountered in our experiments
- $S - C \neq \{\}$



- Compared constraint-based and sequence-based generation
 - Five data structures with “natural” constraints
 - Four different cases
- Constraint-based generation is valuable for bounded-exhaustive generation but can result in false alarms
- Sequence-based generation does not require writing constraints but makes it hard to provide guarantees about bounded-exhaustive testing